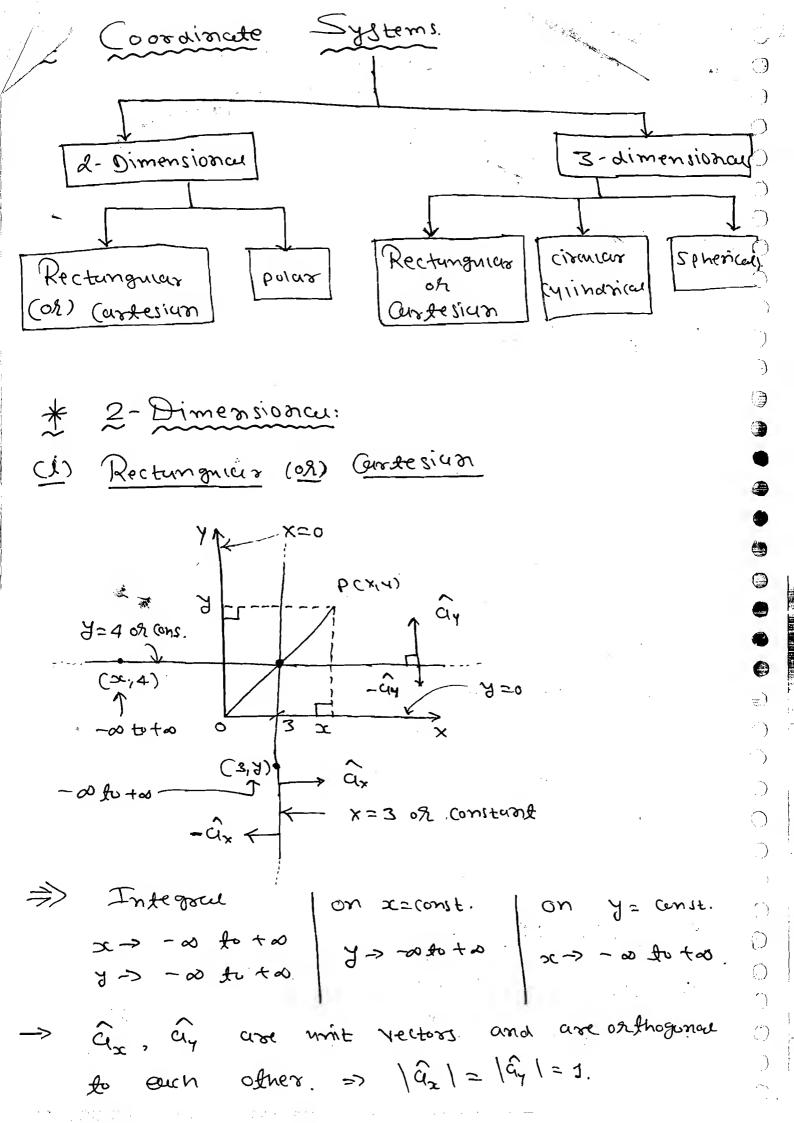
(+918/21564132) ECE PMI(B) MANAGEMENT . Electromagnetic Theory Zis: Koffe? Maser Books -> william Hyte Sudia Ku Edminister -> manapatou & manapatora -> R.F. Haroundfor -> Fraun & Burmain ()

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& lopics D: 24 06/13 3 vo Static fields (Electrostatics & Steady magnetics). -> The fields are independent of time is called Static Geral. De Time Varying beal -> Maxwell Ean. EM Waves. - Dety: -> A wave is a physical phenomena Which reproduces After Certain instant 06 time get some other place, the lime delay bet the prior to the luter locations es proportional to touvelled distance. The whole phenomena consitutes a wave. Therefore, an Em waves is () not only by of time but also a to .) of distunce. Insted ob distunce we (, use space (o-ordinates. (: Wavegnide (Rectangular) Dasics of Antermas O Two wive toursmission lines.

Scattering Parameters.

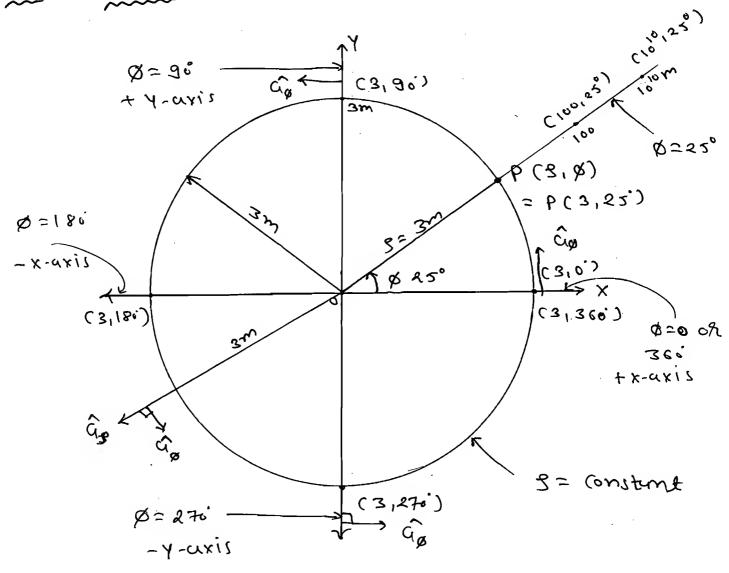


-> They are represented + x -axis and along

y-ciris sespectivery.

-> They may be also represented as unit vectors normal to X= constant and J= constront respectively.

(ii) Polar



-> Locus of 9= constant represents a circuite. Whose Centre Coinsides Should not Oxigion. Therefore, g assumes all possible Vaines sunging from a to 00. All B= constant, & assumess an possible values sunging from o to att.

provide the contract of the co

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Integrais	on 2= con1+.	an & = con ?+.
8 -> 0 to 200	Ø → o to 2π	g - otra.

Dut from the origin. & assumes an possible values sanging from 0 to 2TT.

On & = Constant & assumes all possible values from 0 to 0.

Values sanging from 0 to 0.

The each other

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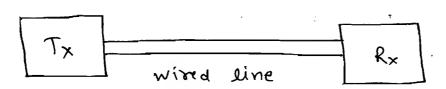
(08) normal to the circle.

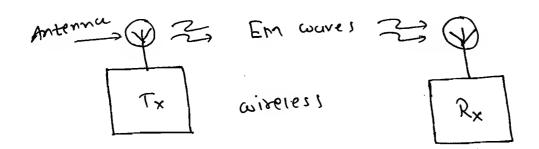
similiany, a_{\varnothing} is a unit vector projecting normal to $\varnothing = constant$. and it is projecting in the Counter clock wise direction by shown in figure.

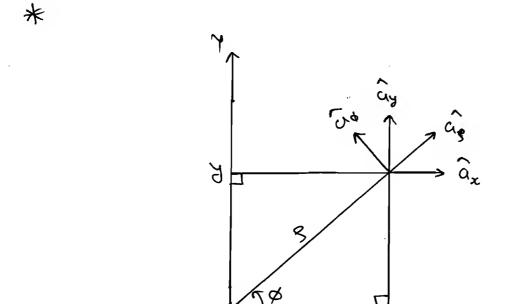
as is tungent to the circle and

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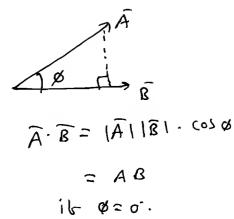
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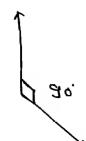
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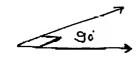


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ay	sin ø	C0 S Ø	0
a ₂	0	0	1

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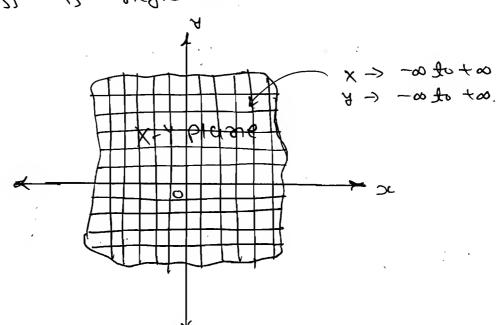


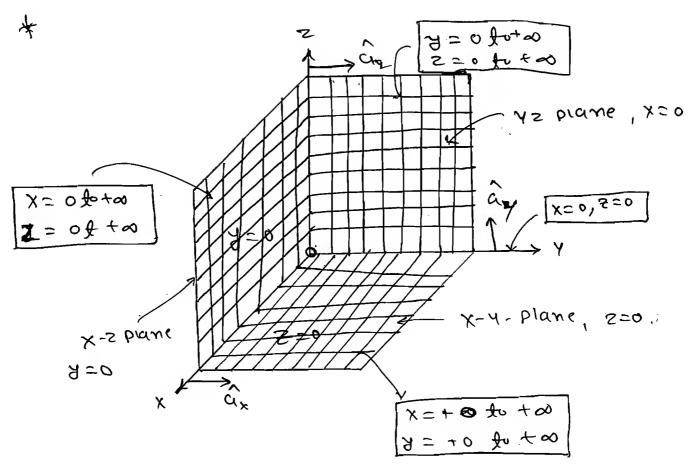


* Plane:

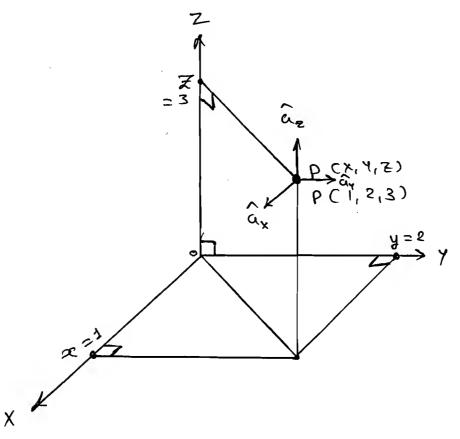
-> Plane is a Sheet like Structure whose

Anickness is neglected.





* Cartesian Gordinates System



To general in a 3-0 Co-ordinates System bixing 3 coordinates that represents a point

2 coordinates that represents a line 1 (0-ordinates that represents a plane. Hixing In general x -> - 00 to +00 y > - 00 to +00 -a to t∞ => a2, a3, a2 are unid vectors of the gonal to each other. $|\hat{a}_{x}| = |\hat{a}_{y}| = |\hat{a}_{z}| = 1.$ => âx, ây, and âz are unit vectors of the gona to each other. -> They use sepresented along x-uxis, y-uxis and s-axis. - They may be also represented as unit vectors normal to x = constant, J= constant, z= Constant planes respectively. O vector/x-axis coming on of the paper

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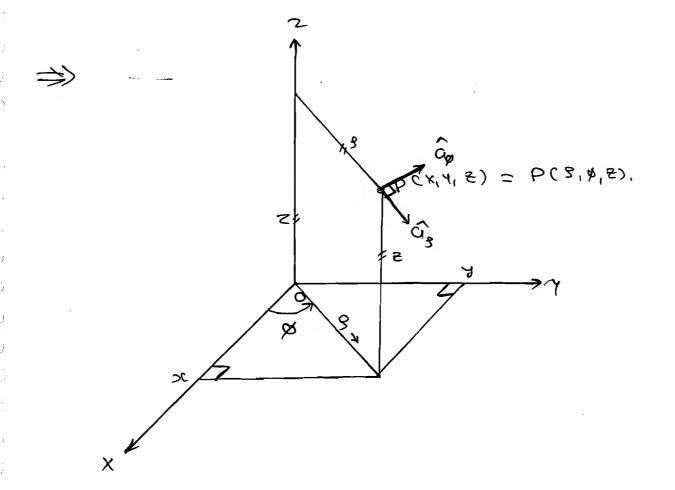
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* [vectors | xis Gring out ob the Paper.

* Circular or Mindrical

Coordinate System.



→ P= constant represents a chiratrical plane whose whose cross-section is circular and whose crois coincides with z-axis rather P is the distance measured normal to z-axis. I can assume all possible ranges, ranging from a to to too.

→ âg is a unit vector projecting mormal

to g= Constant prane.

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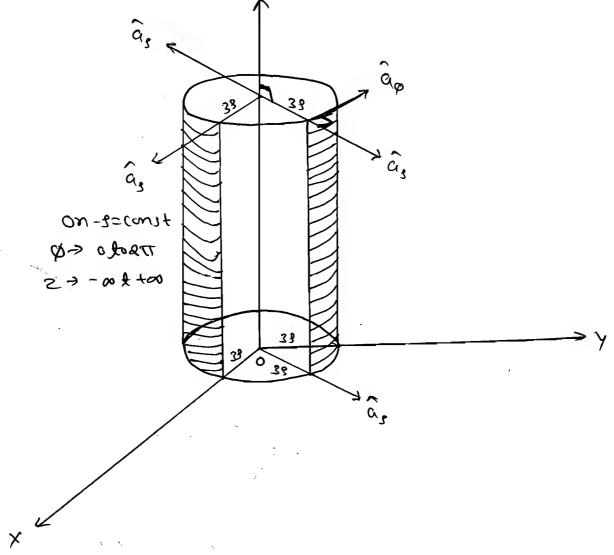
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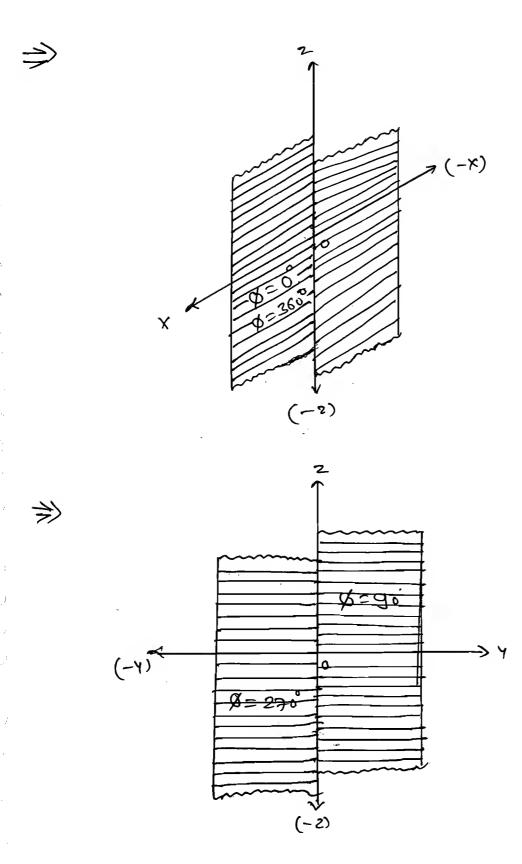


-) of is, called asimuth angre.

-> Ø= constant plane is called elivation Plane.

-> personnes au posibble values sunging born ot att.

of is a unit vector projecting normal to \$= constant plane.

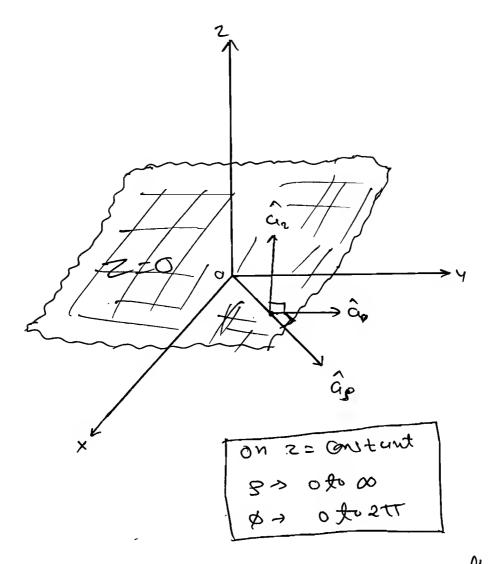


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a persicular Constant plane that Persionice unit vector would projecting normal to the plane they remaining 2 unit vectors and be projecting lungential to the passe.

3 = Constant plane às for e.g. On could be Projecting normal to s=constant and que & que como be projecting tangenties to sur paine.

3

$$\overrightarrow{B} = B_{x} \widehat{\alpha}_{x} + B_{y} \widehat{\alpha}_{y} + B_{z} \widehat{\alpha}_{z} \rightarrow \text{cumbian}$$

$$\overrightarrow{B} = B_{y} \widehat{\alpha}_{y} + B_{y} \widehat{\alpha}_{y} + B_{z} \widehat{\alpha}_{z} \rightarrow \text{cumbanion}$$

Ex-1 Let $\overline{B} = 2\hat{a}_x + 3\hat{a}_y + 4\hat{a}_z$ is define at a point P(3,4,5) m. convert finis vector in chindrical system.

$$\frac{Ans:}{R} = B_s \hat{q}_s + B_\phi \hat{q}_o + B_z \hat{q}_z$$

$$: \overline{B} \cdot \hat{\alpha}_{5} = B_{5} \cdot \hat{\alpha}_{5} \cdot \hat{\alpha}_{5} + B_{6} \cdot \hat{\alpha}_{6} \cdot \hat{\alpha}_{9} + B_{7} \cdot \hat{\alpha}_{7} \cdot \hat{\alpha}_{6}$$

$$\therefore \quad \overline{B} \cdot \hat{a}_{S} = B_{S}.$$

$$B_{S} = \overline{B}. \hat{\alpha}_{S}$$

$$B_s = B \cdot \alpha_s$$

$$B_s = 2 \hat{\alpha}_x \cdot \hat{\alpha}_s + 3 \hat{\alpha}_y \cdot \hat{\alpha}_s + 4 \hat{\alpha}_z \cdot \hat{\alpha}_s$$

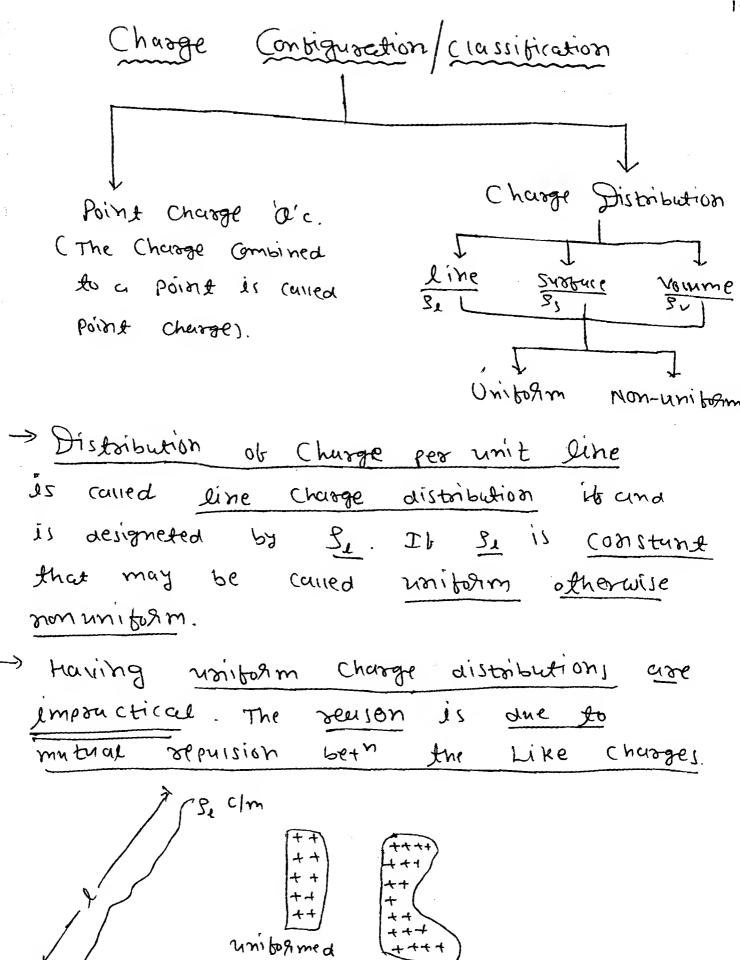
$$B_s = 2 \hat{\alpha}_x \cdot \hat{\alpha}_s + 3 \hat{\alpha}_y \cdot \hat{\alpha}_s + 4 \hat{\alpha}_z \cdot \hat{\alpha}_s$$

Mow, P (3, 4, 5).

similany.

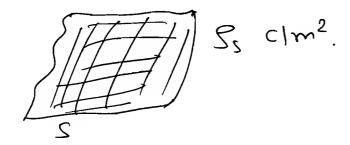
$$B_{\alpha} = \overline{R} \cdot \widehat{q}_{\alpha}, \quad B_{z} = \overline{R} \cdot \overline{q}_{z}$$

$$\therefore \quad \beta \varphi = -2 \sin \varphi + 3 \cos \varphi.$$

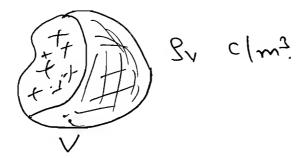


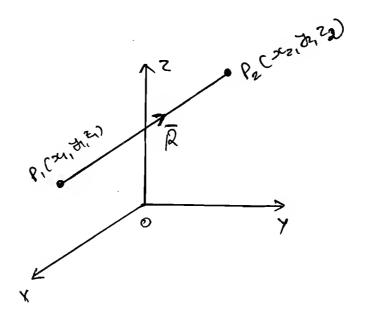
Mon-unifogimed

Distribution of Charge per unit circuit sirent is cared surface charge density, and is designeded by 3_5 c/m²



→ Distribution of Charge per unit Volume is called Volume density and is designed by SV clm3.





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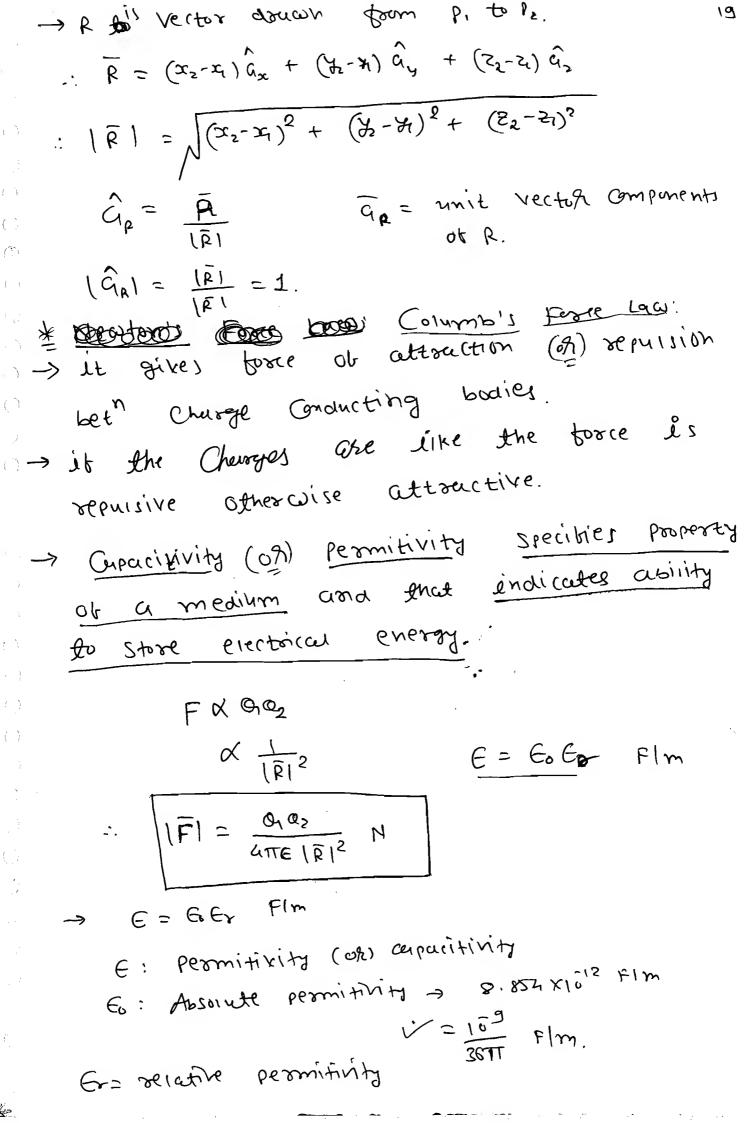
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(a) Diesectoic Constant new to unit.

-> The vector borce on or due on calcons

-> The vector toxer acting on a due to

Ex-1 Four point Churges of John each one located on the xxy axis at tam.

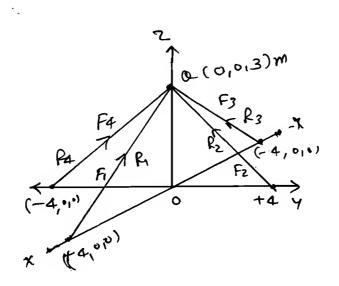
located on the xxy axis at tam.

Find the Vector borre acting on Ima Charge which is located on z-axis

Charge which is located on z-axis

at z=3 meters.

Ams:



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$$-4\hat{q}_x + 3\hat{q}_y$$

$$\overline{F}_{1} = \frac{10 \times 10^{6} \times 10^{3}}{4\pi \times 10^{3} \times (5)^{2}} - \frac{4\hat{q}_{x} + 3\hat{q}_{y}}{(5)}$$

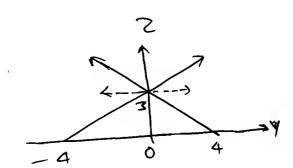
$$\overline{F}_{2} = \frac{10 \times 10^{6} \times 10^{-3}}{4\pi \times 10^{-9} \times (5)^{2}} \times \frac{-4\overline{G}_{4} + 3\overline{G}_{2}}{(5)}$$

$$F_{s} = \frac{10 \times (0^{6} \times (0^{3}))}{4 \times (0^{3} \times (0^{3}))} \times \frac{4 \times (0^{3} \times (0^{3}))}{(5^{3})}$$

$$F_4 = \frac{10 \times 10^7 \times 10^3}{4\pi \times 10^3 \times 10^3} \times \frac{14 \cdot 40^7 + 34 \cdot 20^7}{36\pi}$$

$$F_7 = \frac{10 \times 10^7 \times 10^3}{36\pi} \times \frac{14 \cdot 40^7 + 34 \cdot 20^7}{36\pi}$$

$$F_8 = \frac{10 \times 10^7 \times 10^3}{36\pi} \times \frac{14 \cdot 40^7 + 34 \cdot 20^7}{36\pi}$$



The four Charges are located symmetrically on the x & y axis. about z-axis which result in Concellation of horizontal torre result in Concellation of horizontal torre would components and the resultant torre would be along and airection only.

Ex-2 4 point charges of to each are located at the corners of a Square. What Point Charge to be kept as a centre of a Square So that the resultant force acting on an ouch charge which are located at a corners of a square is Zero. (ON) it is required to hold 4 point charges of to euch in equalibrium at a Square. What Point Charge Corners of to be kept at the contre of the Square So that the Charges would be in equilibrium.

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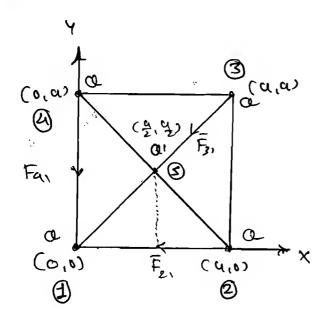
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Hint: equilibrium meurs the resultant borce acting on any charge which are located at the corners of the square is zero.

Ans:



-> We have to find vaine of a in terms of a so that resultant force acting on any charge which are located at the corners of the squale is Zero.

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$$\Rightarrow \overline{F_{e_1}} = \frac{\alpha^2}{4\pi\epsilon(\alpha^2)} \times \frac{-\alpha \hat{u}_x}{\alpha}$$

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$$\widehat{Fa_1} = \frac{a^2}{u\pi\epsilon (a^2)} \times -\frac{u\widehat{ay}}{a}$$

$$\overline{F_{31}} = \frac{\alpha^2}{4\pi^2 (\sqrt{2}\alpha)^2} \times \frac{-\alpha \hat{\alpha}_2 - 6\hat{\alpha}_7}{\sqrt{2}\alpha}$$

$$F_{51} = \frac{\alpha \alpha I}{4\pi \epsilon \left(\frac{G}{52}\right)^2} \times \frac{-\hat{\alpha}_{x} - \hat{\alpha}_{y}}{\sqrt{2}}$$

-> Consider the sum and of as Components of all forces and the same make concested

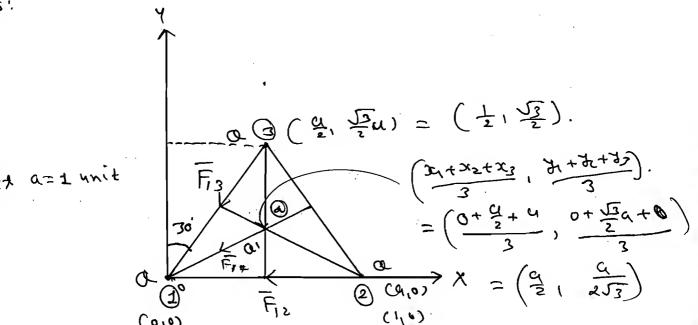
$$\frac{1}{4\pi k a^2} - \frac{0^2}{4\pi k \sqrt{2}a^2} - \frac{001}{4\pi k \frac{a^2}{\sqrt{2}}} = 0$$

-> Exen Ge Consider Ine sum of ay the same ans is expected.

Components

Ex-3 3 point Charges of to each are 10 cated at the corners of a compilateral toicingle. What point charge to be kept the centre or the triumpre so that the seculture force acting on an auch charge which are located at the Comeon of the toiungue is O.

Ams: 01 = - 0



$$\frac{1}{|R|^{2}} = \frac{|R + Q|^{2}}{1} \left(-\frac{\hat{Q}_{x}}{2} - \frac{\sqrt{2}}{2} \hat{q}_{y} \right) = -\frac{\hat{Q}_{x}}{2} \hat{q}_{x} - \frac{\sqrt{2}}{2} \hat{q}_{y} = -\frac{\hat{Q}_{x}}{2} - \frac{\sqrt{3}}{2} \hat{q}_{y}.$$

$$\Rightarrow \overline{F_{12}} = \frac{-k\alpha^2}{1} (\widehat{\alpha}_{\infty}). \qquad \overline{R} = -\widehat{\alpha}_{\infty}$$

$$|\widehat{R}| = 1.$$

$$=) F_{14} = -\frac{k \alpha \alpha 1}{\frac{1}{3}} \times (+\frac{\alpha_{31}}{2} + \frac{1}{2} + \frac{1}{3} + \frac{1}{12} + \frac{1$$

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MOW, Fiz + Fig + Fix = 0.
let, only
$$\hat{q}_{\chi}$$
 - a component

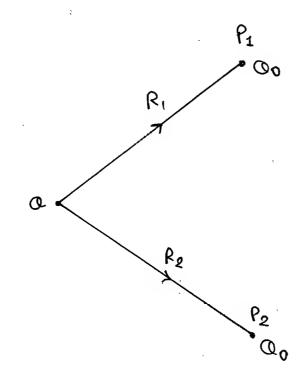
$$-\frac{ka^2}{2} - ka^2 - kaa^1 \times 3\sqrt{3} = 0.$$



$$Q = \frac{-\alpha}{\sqrt{3}} C$$

It we considered only y - component Aven we also get same answers.

- -> It is defined by force per unit Charge.
- -> Unit is M/c (oh) V/m.



$$G$$
 $P_1 \Rightarrow F_1 = \frac{Q}{4\pi\epsilon |\bar{R}_1|^2} \cdot \hat{Q}_{\bar{R}_1} = Eiectoic biend$

$$\rightarrow \overline{F_2} = \frac{Q \cdot Q_0}{4\pi\epsilon |\overline{F_2}|^2} \cdot \widehat{Q_{F_2}}$$

$$\alpha + P_2 \Rightarrow \frac{\overline{F_0}}{\omega} = \frac{\alpha}{4\pi F |\overline{F_2}|^2} \cdot \widehat{G}_{R_2} = \text{Electric Held}$$

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=> Ingenesal

Observation point where we want to find the electric field

Sovere point,

Source or electric Rield is electric charge.

$$\overline{E} = \frac{Q}{4\pi\epsilon l \hat{R} l^2} \cdot \hat{q}_{R}$$

$$\overline{E} = \frac{Q}{4\pi\epsilon l \hat{R} l^2} \times \frac{\hat{R}}{|\hat{R}|^2} \cdot \frac{\hat{R}}{|\hat{R}$$

A point charge of tone is located (0,-4,0) m. An another charge of 20ne is located at (0,0,4) m.

(I) find the electric field at the origin. (ii) Where Should = a zonc point charge to be located so that electric field at oxigin is O.

$$\frac{2}{(0,0,4)}$$

$$\frac{2}{\text{donc}}$$

$$\frac{R_2}{R_3}$$

$$\frac{1}{\text{donc}}$$

$$\frac{2}{R_2}$$

$$\frac{R_2}{R_3}$$

$$\frac{1}{E_3}$$

$$\overline{E}_{1} = \frac{10 \times 10^{9}}{4 \pi F_{0} \times (4)^{2}} \times \frac{4 \cdot \alpha_{y}}{(4)} = 5.625 \cdot \hat{\alpha}_{y} \cdot V \cdot m$$

$$\overline{E_2} = \frac{20 \times 10^9}{4 \times 10^9} \times \frac{-21 \, \text{Gz}}{4} = -11.25 \, \text{Gz}$$
 V/m.

① Electric field at the origin
$$= \overline{E_1} + \overline{E_2} = \left(5.625 \hat{q}_0 - 11.25 \, \hat{q}_2 \right) \, \text{V/m}.$$

$$(2) \quad \overline{E_1} + \overline{E_2} + \overline{E_3} = 0 \Rightarrow \overline{E_3} = -(\overline{E_1} + \overline{E_2}).$$

$$\hat{E}_{3} = - [5.625 \,\hat{q}_{y} - 11.25 \,\hat{q}_{z}] \, \text{V/m}.$$

$$\Rightarrow \overline{E_3} = \frac{30 \times 10^{3}}{4 \pi \times \frac{10^{3}}{3677} \times (x^2 + 4^2 + z^2)^{3/2}} \times (x^2 + 4^2 + z^2)^{3/2} \times \frac{10^{3}}{3677} \times (x^2 + 4^2 + z^2)^{3/2} \times \frac{10^{3}}{3677} \times \frac{10^{3$$

$$\overline{E_{3}} = \frac{d^{20}}{(x^{2}+y^{2}+2^{2})^{3/2}} (-x\hat{a_{x}} - y\hat{a_{y}} - 2\hat{a_{z}})$$

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Compare
$$\hat{a}_{z} \Rightarrow \frac{-270Z}{(\dot{y}^{2}+z^{2})^{31}z} = 11.27 - B$$

$$\frac{A}{B} \Rightarrow -\frac{y}{z} = \frac{1}{z} \Rightarrow \frac{\frac{2}{y} = -2}{y}$$

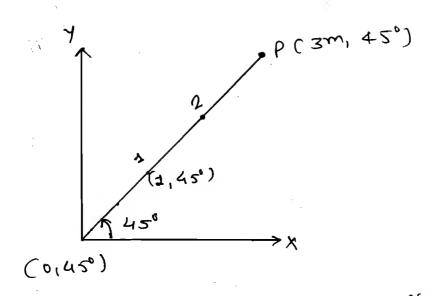
$$\Rightarrow \frac{2707}{3} = 5-625.$$

$$Y = \pm 2.07 \text{ m}$$

$$Z = -27 = \mp 4.14 \text{ m}.$$

The posibilities.

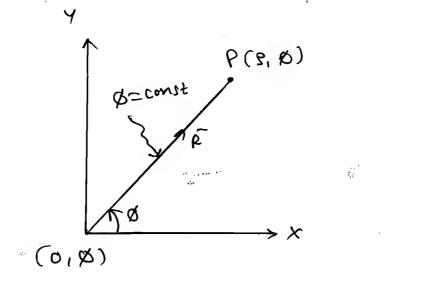
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 \Rightarrow Gie assume that the origin lines on 0 or 0 origin is

- with reb. to P (3m, 45°), the origin is Coordinated as (om, 45°)

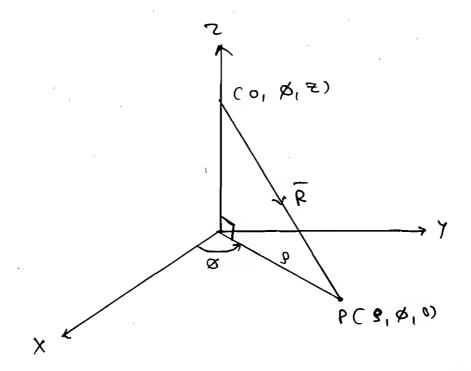


(origin lines on &= Const. time)

$$\overline{\rho} = (9-0) \hat{q}_{g} + (\varnothing-\varnothing) \hat{q}_{g}$$

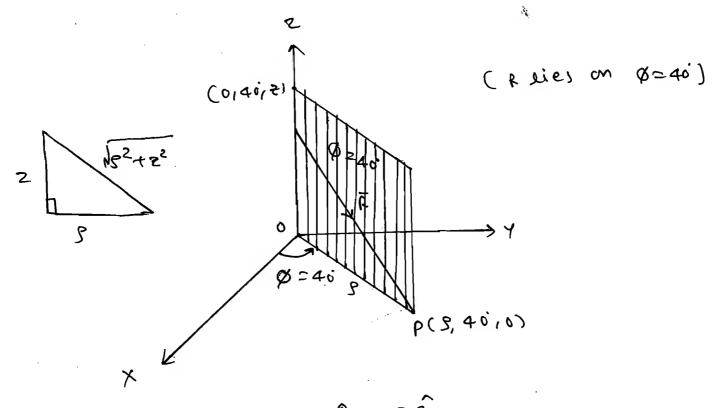
$$|\hat{q}| = |\hat{q}| = |\hat{q}|$$

$$\hat{q}_{p} = |\hat{p}| = |\hat{q}|$$



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 \rightarrow With set to $P(P, \emptyset, 0)$ the point on the Z-axis in (o-orainated α) (0, \emptyset , Z).



-> The point on the z-axis also assumed to wing on Q = 46 plane.

in with set to P (3, 40,0), the point on the z-axis is co-ordinated as (0,40,2).

Ex-1 Expression for E due to a line with a Charge density of Se clm

$$\frac{1}{2} \int_{0}^{R} \frac{dx}{dx} = \frac{dx}{4\pi\epsilon |\vec{R}|^{2}} \int_{0}^{R} \frac{dx}{4\pi\epsilon |\vec{R}|^{2}} \int_{0}^{R$$

→ do= Sedl

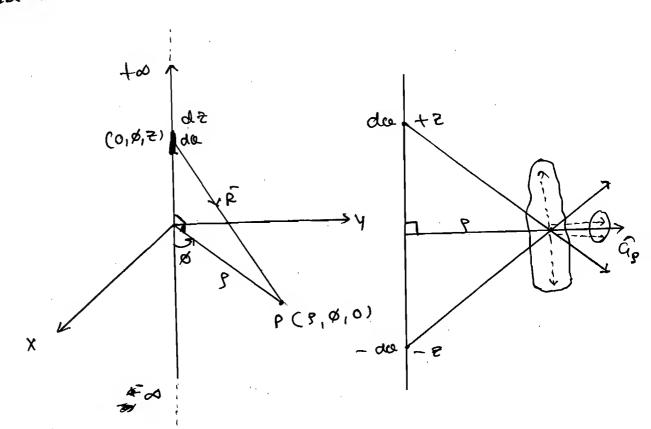
-) We assume that 'dl' is so small such that it shownking to the point. When One say, it is a point, see consider that the 'de' is located then it can have Coordinates.

At this point, we consider that the Ido. is rocated.

(i) Magnitude of the E is inversity propositioned to the distance beth the infinite line and the observation the Point.

(ii) the direction of the E Could be projecting in a directing normal to the infinite line.

Ans: We assume that the infinite line lies along 2-axis. extending from - outoto lies along 2-axis. extending from - outoto are find the electric field at some point on the X-4 plane. For that Convinience we make the circuit cylinarical co-ordinates.



-> do = go dz de > Shownk to point At this point, are assume that 'do' is located. : with 864. (B, B, O), the point on the Z-axis is (0-ordinated as (0,0,0). At this point da is located P = 9 a3 - 2 a2 : $QE = \frac{745}{27456} = \frac{125455}{205-505}$ NOTE: took every da at +2 on the tree z'axis these exist an another do on the -ve z-axis at -z. → The Churge Consignation is symmetry about X-4 plane. Which result in Cancellation of az components and the resultant field amid be along as direction only. i-e--> In general, no field Component exist along the imag length or the line resulting E exists morma to line ignoring az The forted

Component

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:)

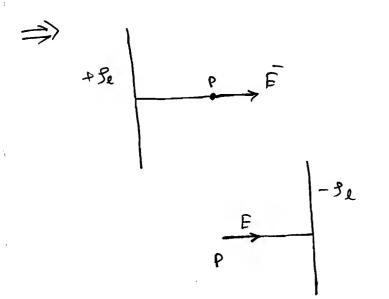
-> The Lotu field given by.

$$\overline{E} = \frac{g_{0}g}{4\pi\epsilon} \hat{G}_{0} \int \frac{dz}{(g^{2}+z^{2})^{3}} \frac{z = g \tan \theta}{(g^{2}+z^{2})^{3}} Z = g \sin^{2}\theta d\theta$$

$$= \frac{g_{0}g}{4\pi\epsilon} + \frac{g_{0}g}{(g^{2}+z^{2})^{3}} = \frac{g^{2}}{g^{2}} + \frac{g^{2}}{g^{2}} = \frac{g^{2}}{g^{2}} = \frac{g^{2}}{g^{2}} + \frac{g^{2}}{g^{2}} = \frac{g^{2}}{g^{2}} + \frac{g^{2}}{g^{2}} = \frac{g^{2}}{g^{2}} = \frac{g^{2}}{g^{2}} = \frac{g^{2}}{g^{2}} = \frac{g^{2}}{g^{2}} + \frac{g^{2}}{g^{2}} = \frac{g^{2}}{g^{2}$$

$$= \frac{Se}{2\pi F S} \xrightarrow{\alpha_g} \Rightarrow \left[\frac{\hat{E} | \alpha_g}{S} \right]$$

-> where, 'p' is the distance blue the infinite line and the observation point.



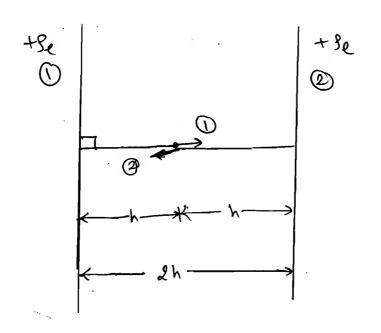
→ It Be is the direction of E comed be away from the infinite line.

→ It Be is -ve the direction of the E

would be towards the infinite line.

I Two infinite lines are parounel they are superated by et man (n70). They are distributed with united me Line charge desity of the clomench. Find mag. of the electric field. beth this infinite line and also find direction of the electric field.

Ans:



[[E1=0] in defining the direction of F.

Ex-? Repeat the above problem it they are distributed with +9, Clm and -3e clm

Ans:

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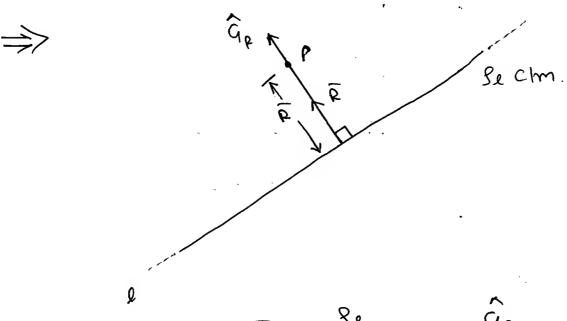
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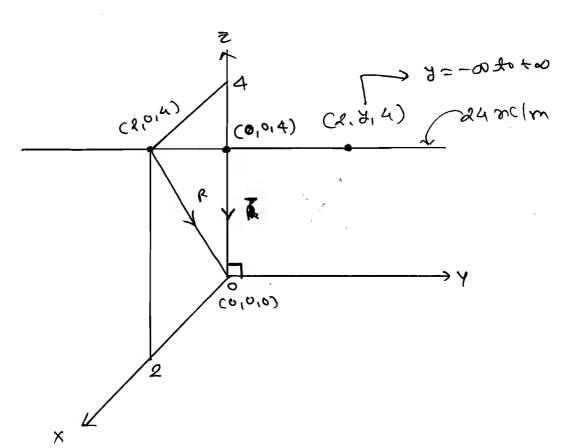
-> The direction of E would be Loward the line which is having - Se clm.

Expression tor E due to an arbitary oriented infinite sine with a unitorym Charge density of Se clm.



Ex- $\frac{1}{2}$ Find expression to the electric field at (a) origin (b) (4,516) m (c) (10,10,10) m. due to an infinite line with unitedm charge density of 24 nc/m. Which lies at x=2, y=4m.

Ans.



D et ongin

$$\therefore \overline{R} = -2 \dot{q}_{x} - 4 \dot{q}_{z}$$

$$\overline{E} = \frac{24 \times 10^{8}}{271 \times 10^{8}} \times \sqrt{10}$$

$$93197 \times \sqrt{10}$$

$$= \frac{216 \times 2}{20} \times (-20 \hat{x} - 40 \hat{a}_{2})$$

$$= \frac{216 \times 2}{20} \times (-20 \hat{x} - 40 \hat{a}_{2})$$

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$$= \frac{216 \times 2}{20} \times (-20 \hat{x} - 40 \hat{a}_{2})$$

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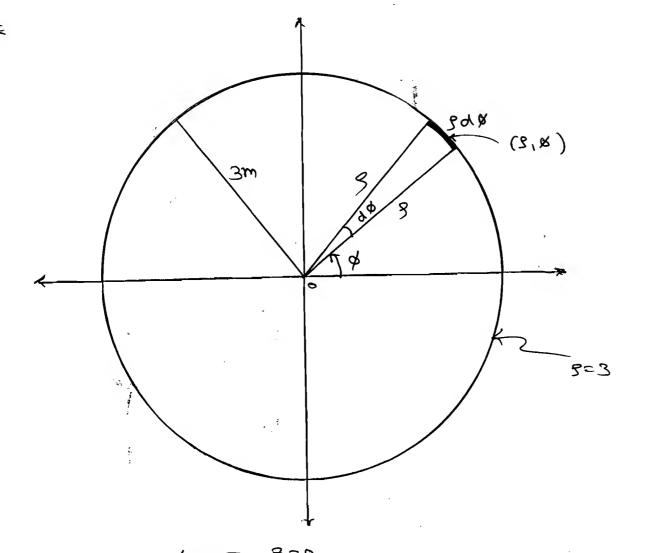
\) \

$$= \frac{2^{2} \times 10^{9}}{2^{18} \times 10^{2}} \times \sqrt{8} \times 2^{\frac{2}{3}} \times \sqrt{8}$$

$$\frac{E > 54 (2\hat{q}_x + 2\hat{q}_z)}{E = 108(\hat{q}_{xi} + \hat{q}_z)}$$
 V/m

$$\frac{1}{183577} = \frac{24 \times 10^{9}}{24 \times 10^{9}} \times \frac{8\hat{q}_{x} + 6\hat{q}_{z}}{10}$$

$$E = 4.32 (8\hat{a}_x + 6\hat{a}_z)$$
 VIm



$$\rightarrow$$
 9=3, $0 \le 0 \le 2\pi$, $z=0$
 \Rightarrow This represents, there exists a circle of radius zm (entered at origion and is located in $z=0$ pieme.

$$de = 3d\emptyset.$$

$$e = 3d\emptyset = 3 \int_{0}^{\infty} d\emptyset = 6\pi m.$$

$$(200, 303)$$

dl > 80 small such that it is smarking to a point (i.e) dø > 0.

Then, that point is considered as (P, Ø).

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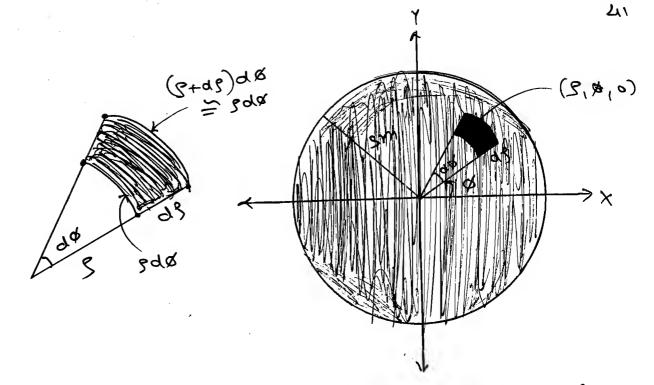
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→ 0 0 ≤ 3 ≤ 3, 0 ≤ 8 ≤ 27, 2=0 This sepresents a circular disk of 0 5 53, 2 =0

oudins 3m, centered il bomo rigino to located in Z=0 purse.

925 69698 S = 3 3 3 ds do $= \int_{S} S[\infty]^{2\pi} d\theta.$ = \(\gamma \) (2\pi) \(3\) \(3\) \(3\) = [32] 3 x 29T 5 = 9TT m2

ds -> 80 small such that it snownks to a point (i-e) ds→0, dø→0. : That point is coordinated as (3,8) of (3,8,0).

* Electric fierd (E) due to a Sheet with a unitorm Charge density of Ss c/m².

 \Leftrightarrow

A. T.

da = 9, ds

S C m²

ds -> Shownk to a point,

At this point, we consider that 'do' is located. When we say, it is a point,

then it am have co-orainates.

$$\frac{1}{E} = \int \frac{3 ds}{4\pi E |\bar{p}|^2} \times \frac{\bar{R}}{|\bar{R}|} \times |m|$$

donne integora.

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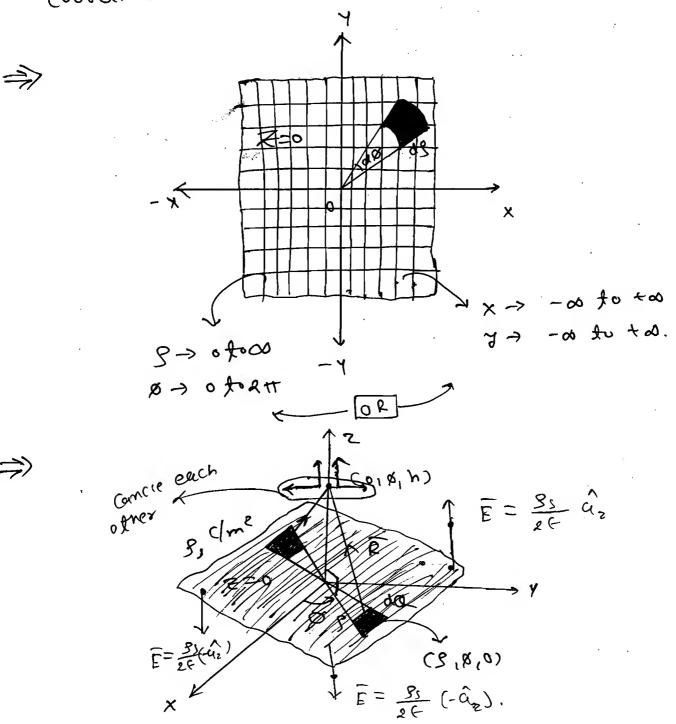
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Ex-1 Find an expression for the E due unitorim to an institute sheet whith the unitorim Charge density of So (Im? #

(accepted in the Z=0 plane. We find the E at some point an the Z-axis. For the Convinere we use cylindrical coordinates.



ds = 8 ds dx. de= 5, d1 da = 3, 3 d3d8 ds -> Shownes to a point point in coordinated as (P, P, O) [orab,ocepo oi] At this point 'do' is lucated, $dE = \frac{S_3.9 ds d8}{4\pi \epsilon (\sqrt{s^2 + h^2})^2} - \frac{-9\hat{q}_s^2 + h\hat{q}_s^2}{\sqrt{s^2 + h^2}}$ As snown in figure top every de on the Sheet there exists an another do diametrically Oposite Side. Therefore, the Charge Configuration is Symmetry about 2-axis. which results in concellation of horizontal bierd components. And the resultant E Gond be along az direction only. i.e. No field component exists 11th to the infinite Sheet. The resultant billid exists in the disection to the normal to the sneed here, ignoring que components. The fotus

field is given 5%,

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-> Ignoring a, component.

beld is 2462 PA the total

$$E = \frac{3^{1}h}{41115} \hat{C}^{3} \int_{0}^{\infty} \frac{65 + k^{2}}{315}$$

$$\int_{0}^{8\pi} dp = 2\pi$$

$$\int_{0}^{8\pi} \frac{gds}{(g^{2}+h^{2})^{3}lz} = \frac{1}{h}.$$

pul 3+ h = t.

: 23d3=at

th = 262 :

$$\frac{1}{E} = \frac{S_s}{2E} \hat{q}_z \quad Vlm$$

$$\rightarrow$$
 In, general $\frac{1}{E} = \frac{95}{26} \hat{a}_n Vlm$

Where, an is the mormal unit vector at the Observation point with set. to infinite sheet.

-> It Bs is +ve, the direction of E would be

away born the infinite Sheet.

-) It 8, is -ve, the direction of E would be toward to the infinite Sheel.

Ex-1 Two Infinite Sheeks are 11th, Inex are Separated by 2h m. they are distributed with uniform Charge density of 5, clm2 Cuch find the electric field at any Point beth this two infinite Sheek.

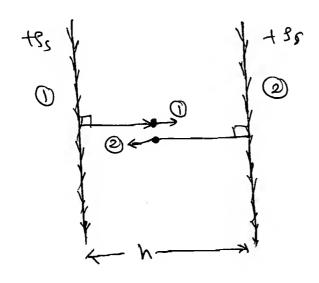
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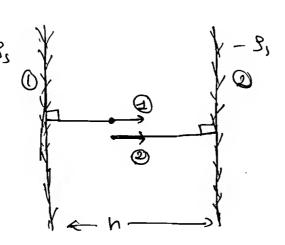
Ans:



The helds add in out of phase.

Ex-2 Repeate the above example It they are distributed with uniform charge density at +35 c/m² and -3, c/m². The

Ans:

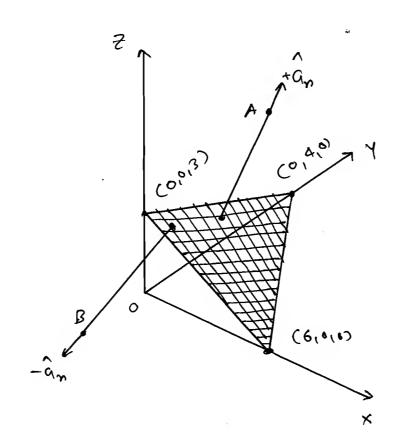


The fields add in in-phase.

The direction of E would be founded the Sheek which is having -9, clm2.

Ex-3 An Intinite Sheet with a uniterm Charge density of let nc/m^2 is ries in a prane define by 2x+3y+4z=12. Find the E in an the regions.

Ans:



$$E (at B) = \frac{g_s}{2E} \hat{a}_n$$

$$E (at B) = \frac{g_s}{2E} (-\hat{a}_n)$$

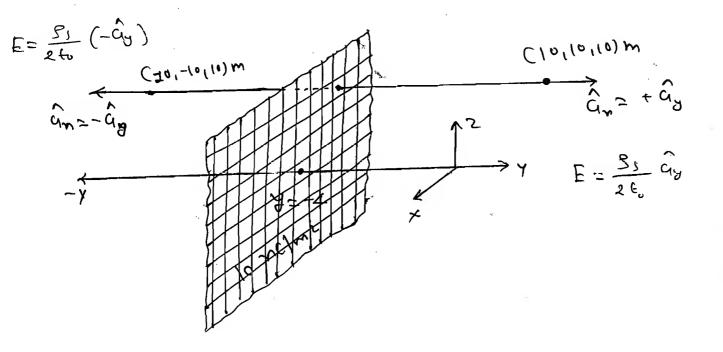
$$\hat{a}_{n} = \frac{2\hat{a}_{x} + 3\hat{a}_{y} + 4\hat{a}_{y}}{\sqrt{2^{2} + 3^{2} + 4^{2}}}$$

Ex-4 An Infinite Sheet with a unitarm Charge density of 10 nclm2 is ines at y=-4m.

Find the E at (10,10,10)m

(i) (10,10,10)m (ii) (10,-10,10)m.

The inhinite sherf is nel to z-x pique.



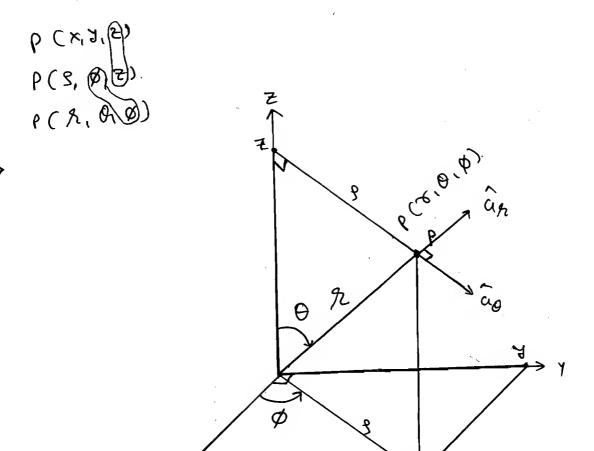
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(i) at $C(0)(0)^{2}$ $\overline{E} = \frac{S_{5}}{2E} \widehat{a}_{y} \quad Vlm$

(ii) at (10_1-10_110) $\overline{F} = \frac{9_5}{2E_0} (-\hat{q}_y). V]m.$





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$$\theta = (05)(\frac{2}{h}) \quad 0 \leq 0 \leq 17$$

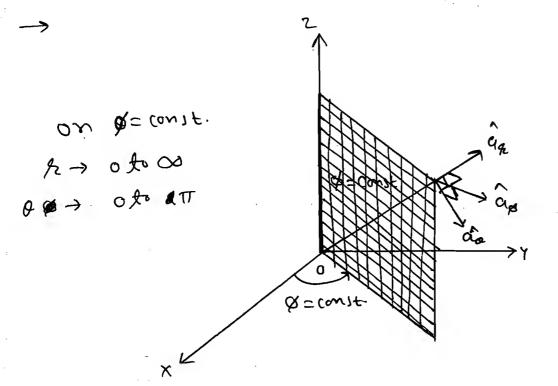
$$\emptyset = fan'(\frac{y}{2}) \quad 0 \le \emptyset \le 2\pi$$

-> Locus ob 9= Constant represents a sprese (or) a spresicercia whoes centre coinsides with the origin. Therefore, & assume all \cdot Possible raines sanding from ato a (\cdot) \bigcirc -> ag is a unit vector projecting normal \bigcirc to 2= constant (OR) normal to the Sphere. aiso (aired Radia disertion. of 97-const. A -> otoTT Ø > Of ATT \bigcirc \bigcirc Si 10=30 a_o on o= const. 8 → o th & profest) 8g Х,

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-> As snown in the figure a assymes all Possible values sunging born of T

-> Ge is a unit vector projecting normal to 0 = constant plane. Further, an, an, orthogonal to each other.



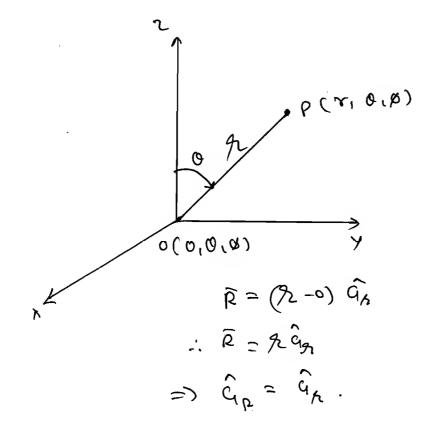
-> & cizzame? all bozzipie raine? sanding from o to RT. and is a unit vector projecting normal to &= const. plane. fundmer ar write âx, ûx and ûx are orthogonal to even other.

→ Ø= Const. Plane is Clisa (alled Elevation

plane.

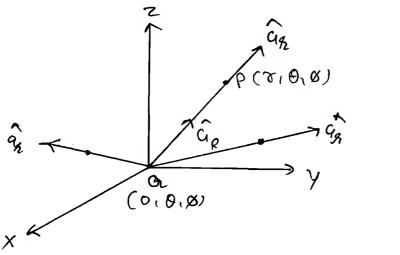
O- with set to P (5,0,0) what are the co-ordinates of the oxigin. ?

(A) = (0,0(x).



Q-1 A point Charge of a Colombs 10 (ated at the origin find E at a distunt point P in Sprenicu co-ordinates.

Ans:



$$\widehat{E} = \frac{Q}{4\pi E |\widehat{P}|^2} \cdot \widehat{Q}_{\widehat{p}}$$

$$= \frac{Q}{4\pi E \Re^2} \cdot \widehat{Q}_{\widehat{g}}.$$

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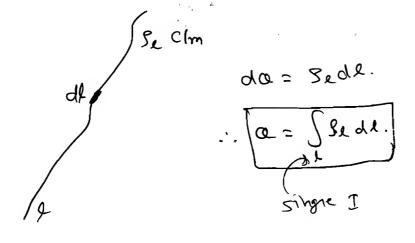
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- . I > Thus, the disection of E would be along sadial (A) an disection,

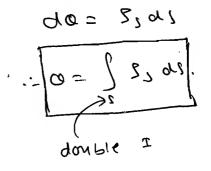
* Total charge (aichiation:

(1) Line Churge:

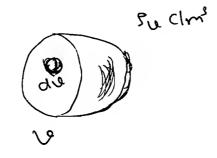


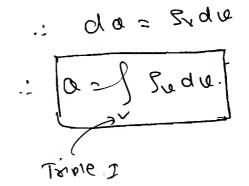
(2) Surface Charge

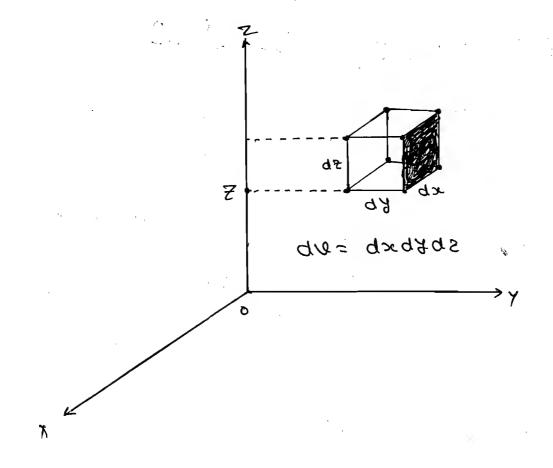


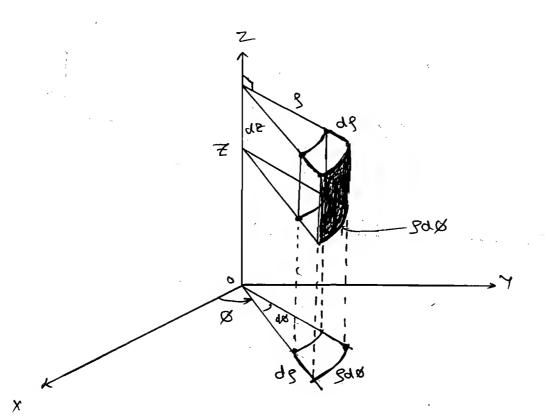


(3) Volume Charge

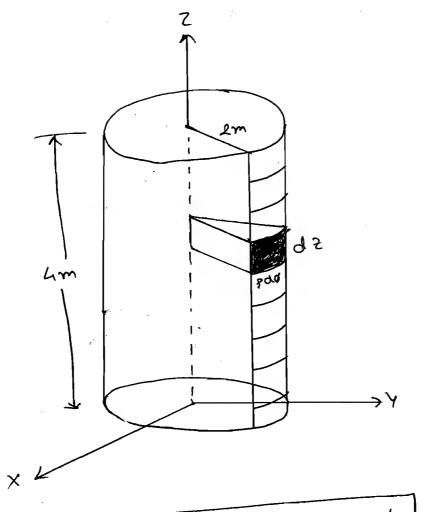








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97= 29005

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(x) (z)

(x) (z)

AThis depresents a cylindrical sheet with sudily 2m and height 4m.

... J = 2(21T)(4)m.

5=16TT m2

Ex-1 Find the total charge with in each or the volume indicate below:

(1) $S_V = 102^{\frac{1}{2}}e^{-0.1}x$ sintly nclm³ $0 \le x \le 1$, $1 \le y \le e$, $2.5 \le z \le 4.5$.

3 50 = 10 e e nc/m3; Ist octums.

Ams: du = docatae.

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(1) $Q = \int_{0}^{2} \int_{0}^$

 $O = \frac{1}{2}O \times \left[\frac{e}{-0.1}\right]_{0}^{2} \times \left[-\frac{1}{2}\right]_{1}^{2} \times \left[\frac{2}{3}\right]_{2.5}^{4.5}$

 $\frac{1}{2} = \frac{1}{2} \times \left[\frac{e^{-1}}{e^{-1}} \right] \times \left[\frac{1+1}{4} \right] \times \left[\frac{(4.5)^3 - (2.5)}{3} \right]$

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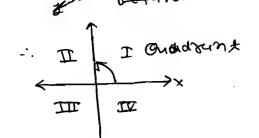
: 0 = ___.

S == Bcolk' &=Bzina

: 30 = 82 sinzø. 22 no/m2.

$$\therefore \alpha = \left[\frac{84}{4}\right]_0^2 \times \left[\frac{-(012)}{2}\right]_0^{1/2} \times \left[\frac{23}{3}\right]_0^1$$

$$= \left[\begin{array}{c} 2 \\ \cancel{X} \\ \cancel{X} \end{array} \right] \times \left[\begin{array}{c} 1 \\ \cancel{X} \end{array} \right].$$



I- Ouadrant: X, y are the

du= gasapaz.

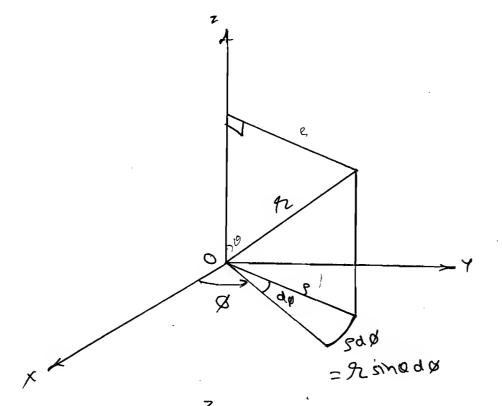
$$0 = 10 \int_{0}^{\infty} \int_{0}^{\pi/2} \int_{0}^{\pi/2}$$

$$\int_{0}^{\infty} e^{-i\omega S} dS \times \int_{0}^{\infty} d\varphi \times \int_{0}^{\infty} e^{-i\omega S} d\varphi = 0$$

$$\therefore Q = J_0 = \int_0^{-\frac{1}{2}} \frac{e^{-\frac{1}{2}}}{e^{-\frac{1}{2}}} + \left(1\right) \frac{e^{-\frac{1}{2}}}{e^{-\frac{1}{2}}} = \int_0^{\infty} \left(\frac{e^{-\frac{1}{2}}}{e^{-\frac{1}{2}}}\right) \frac{e^{-\frac{1}{2}}}{e^{-\frac{1}{2}}} = \int_0^{\infty} \left(\frac{e^{-\frac{1}{2}}}{e^{-\frac{1}2}}\right) \frac{e^{-\frac{1}{2}}}{e^{-\frac{1}{2}}} = \int_0^{\infty} \left(\frac{e^{-\frac{1}{2}}}$$

$$= \frac{1}{4} \left[\begin{array}{c} 0 + \frac{1}{100} \\ 0 \end{array} \right] \times \left[\begin{array}{c} 1 \\ 2 \end{array} \right] \times \left[\begin{array}{c} 1 \end{array} \right] \times \left[\begin{array}{c} 1 \\ 2 \end{array} \right] \times \left[\begin{array}{c} 1 \end{array} \right] \times$$

$$\therefore \boxed{a = +\frac{1}{20}, \text{ nc}}$$



 $dS = RdQ \cdot R \sin \theta \cdot d\theta$ $dS = RdQ \cdot R \sin \theta \cdot d\theta$ $R \sin \theta \cdot d\theta$ $R \sin \theta \cdot d\theta$ $R \sin \theta \cdot d\theta$

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=> 9=2m, 0 ≤ 0 ≤ TT, 0 ≤ 8 ≤ 2TT

=> This represents a sphere of 2m centered at origin.

ds = Re sinoda a8

$$\frac{\pi}{s} = \int_{0}^{\pi} \int_{0}^{2} \sin \alpha d\alpha d\beta$$

$$\cos \alpha \cos \alpha \cos \alpha \cos \alpha$$

$$\cos \alpha \cos \alpha \cos \alpha \cos \alpha$$

:= S= 4T(2) m?.

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Ex-1 Leti $Su = \frac{4}{3} \frac{\cos^2 \theta \cdot \sin^2 \theta}{R^2(R^2+1)}$ de time top universe.

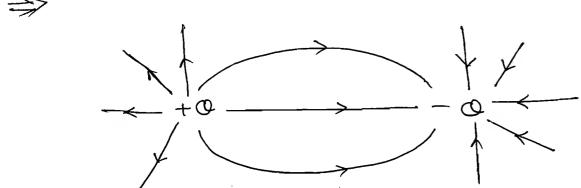
Find the total charge.

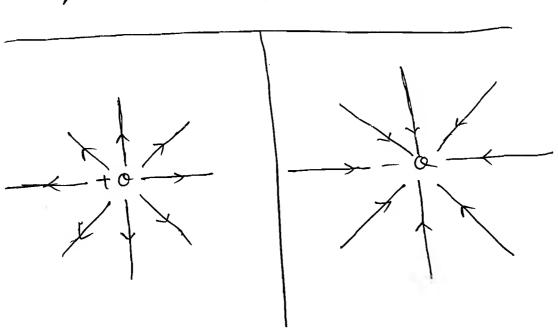
du=92 sino dod.

$$0 = \int \int \int \int \int \frac{dx}{3} \cdot \frac{(0)^2 0 \cdot \sin^2 \theta}{9 x^2 (x^2 + 1)} \times \frac{1}{3} \cdot \frac{(0)^2 0 \cdot \sin^2 \theta}{9 x^2 (x^2 + 1)} \times \frac{1}{3} \cdot \frac{(0)^2 0 \cdot \sin^2 \theta}{9 x^2 (x^2 + 1)} \times \frac{1}{3} \cdot \frac{(0)^2 0 \cdot \sin^2 \theta}{9 x^2 (x^2 + 1)} \times \frac{1}{3} \cdot \frac{(0)^2 0 \cdot \sin^2 \theta}{9 x^2 (x^2 + 1)} \times \frac{1}{3} \cdot \frac{(0)^2 0 \cdot \sin^2 \theta}{9 x^2 (x^2 + 1)} \times \frac{1}{3} \cdot \frac{(0)^2 0 \cdot \sin^2 \theta}{9 x^2 (x^2 + 1)} \times \frac{1}{3} \cdot \frac{(0)^2 0 \cdot \sin^2 \theta}{9 x^2 (x^2 + 1)} \times \frac{1}{3} \cdot \frac{(0)^2 0 \cdot \sin^2 \theta}{9 x^2 (x^2 + 1)} \times \frac{1}{3} \cdot \frac{(0)^2 0 \cdot \sin^2 \theta}{9 x^2 (x^2 + 1)} \times \frac{1}{3} \cdot \frac{(0)^2 0 \cdot \sin^2 \theta}{9 x^2 (x^2 + 1)} \times \frac{1}{3} \cdot \frac{(0)^2 0 \cdot \sin^2 \theta}{9 x^2 (x^2 + 1)} \times \frac{1}{3} \cdot \frac{(0)^2 0 \cdot \sin^2 \theta}{9 x^2 (x^2 + 1)} \times \frac{1}{3} \cdot \frac{(0)^2 0 \cdot \sin^2 \theta}{9 x^2 (x^2 + 1)} \times \frac{1}{3} \cdot \frac{(0)^2 0 \cdot \sin^2 \theta}{9 x^2 (x^2 + 1)} \times \frac{1}{3} \cdot \frac{(0)^2 0 \cdot \sin^2 \theta}{9 x^2 (x^2 + 1)} \times \frac{1}{3} \cdot \frac{(0)^2 0 \cdot \sin^2 \theta}{9 x^2 (x^2 + 1)} \times \frac{1}{3} \cdot \frac{(0)^2 0 \cdot \sin^2 \theta}{9 x^2 (x^2 + 1)} \times \frac{1}{3} \cdot \frac{(0)^2 0 \cdot \sin^2 \theta}{9 x^2 (x^2 + 1)} \times \frac{1}{3} \cdot \frac{(0)^2 0 \cdot \sin^2 \theta}{9 x^2 (x^2 + 1)} \times \frac{1}{3} \cdot \frac{(0)^2 0 \cdot \sin^2 \theta}{9 x^2 (x^2 + 1)} \times \frac{1}{3} \cdot \frac{(0)^2 0 \cdot \sin^2 \theta}{9 x^2 (x^2 + 1)} \times \frac{1}{3} \cdot \frac{(0)^2 0 \cdot \sin^2 \theta}{9 x^2 (x^2 + 1)} \times \frac{1}{3} \cdot \frac{(0)^2 0 \cdot \sin^2 \theta}{9 x^2 (x^2 + 1)} \times \frac{1}{3} \cdot \frac{(0)^2 0 \cdot \sin^2 \theta}{9 x^2 (x^2 + 1)} \times \frac{1}{3} \cdot \frac{(0)^2 0 \cdot \sin^2 \theta}{9 x^2 (x^2 + 1)} \times \frac{1}{3} \cdot \frac{(0)^2 0 \cdot \sin^2 \theta}{9 x^2 (x^2 + 1)} \times \frac{1}{3} \cdot \frac{(0)^2 0 \cdot \sin^2 \theta}{9 x^2 (x^2 + 1)} \times \frac{1}{3} \cdot \frac{(0)^2 0 \cdot \sin^2 \theta}{9 x^2 (x^2 + 1)} \times \frac{1}{3} \cdot \frac{(0)^2 0 \cdot \sin^2 \theta}{9 x^2 (x^2 + 1)} \times \frac{1}{3} \cdot \frac{(0)^2 0 \cdot \sin^2 \theta}{9 x^2 (x^2 + 1)} \times \frac{1}{3} \cdot \frac{(0)^2 0 \cdot \sin^2 \theta}{9 x^2 (x^2 + 1)} \times \frac{1}{3} \cdot \frac{(0)^2 0 \cdot \sin^2 \theta}{9 x^2 (x^2 + 1)} \times \frac{1}{3} \cdot \frac{(0)^2 0 \cdot \sin^2 \theta}{9 x^2 (x^2 + 1)} \times \frac{1}{3} \cdot \frac{(0)^2 0 \cdot \sin^2 \theta}{9 x^2 (x^2 + 1)} \times \frac{1}{3} \cdot \frac{(0)^2 0 \cdot \sin^2 \theta}{9 x^2 (x^2 + 1)} \times \frac{1}{3} \cdot \frac{(0)^2 0 \cdot \sin^2 \theta}{9 x^2 (x^2 + 1)} \times \frac{1}{3} \cdot \frac{(0)^2 0 \cdot \sin^2 \theta}{9 x^2 (x^2 + 1)} \times \frac{1}{3} \cdot \frac{(0)^2 0 \cdot \sin^2 \theta}{9 x^2 (x^2 + 1)} \times \frac{1}{3} \cdot \frac{(0)^2 0 \cdot \sin^2 \theta}{9 x^2 (x^2 + 1)} \times \frac{1}{3} \cdot \frac{(0)^2 0 \cdot \sin^2 \theta}{9 x^2 (x^2 + 1)} \times \frac{1}{3} \cdot \frac{(0)^2 0 \cdot \sin^2 \theta}{9 x^2 (x^2 + 1)} \times \frac{1}{3} \cdot \frac{($$

$$=\frac{4}{3}\left[\frac{4}{3}\ln^{3}3\right]^{8}\times\left[-\frac{\cos^{3}8}{3}\right]^{7}\times\left[\frac{8}{2}-\frac{\sin^{2}8}{3}\right]^{27}$$

$$=\frac{4}{3}\left[\frac{\pi}{2}\right]\times\left[\frac{1}{3}+\frac{1}{3}\right]\times\left[\frac{\pi}{3}\right].$$





-> An Electoic flux originales from a tre

(harge and end) with a negative (harge.

In the absence of -ve charge electric

flux terminates at intinity.

Churge could result ob electric 61 1 C erector bux. outher con IC OF ac or electric Charge would result electro(Gux. O- C 06

Ex-1 How much Elector forx would result from a non-uniform surface charge density 3 nc/m² define for 9 5 5m,

$$S = 0 \quad \text{S} = 0$$

$$S = 0 \quad \text{S} = 0$$

$$S = 0 \quad \text{S} = 0$$

Z=4m

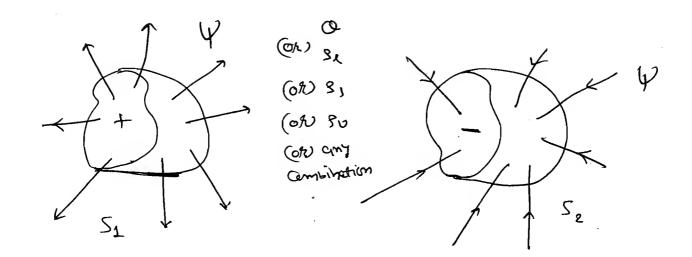
$$\psi = \left[[5] - \left[\frac{1}{2} \ln^{-1} S \right] \right] \times 2\pi$$

$$\psi = \left[[5] - \left[\frac{1}{2} \ln^{-1} S \right] \times 2\pi \right] \times 2\pi$$

$$\psi = \left[[5] - \frac{1}{2} \ln^{-1} S \right] \times 2\pi$$

$$\psi = \left[[5] - \frac{1}{2} \ln^{-1} S \right] \times 2\pi$$





51 8 52 = arbitary Closed systemes.

Unex = Qenc.

Si & Some two assistany Closed

Susfaces. We assume that they enclosed

Some Charge Contiguration i.e. either

O (and Se (or) S. (or) Se (or) any Combination

Some how we use have calculated the

total Charge Widhin them.

Further, we assume that s, encloses the charge which would result thux living surface. The amount of electric flux living surface is equals to the Charge enclosed within it.

Further we assume that Sz encloses -re Charge. Which would Therefore, the Heur enter the closed surface. 0

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- -) weigher the elector blux living the 63 Surface or entering the surface, the electoic Klux Passing through the Closed
- -> Crausi's Law's State that the nex electric blux pussing through any Closed surface is eanous to the charge enclosed by that sustance.

surfuces.

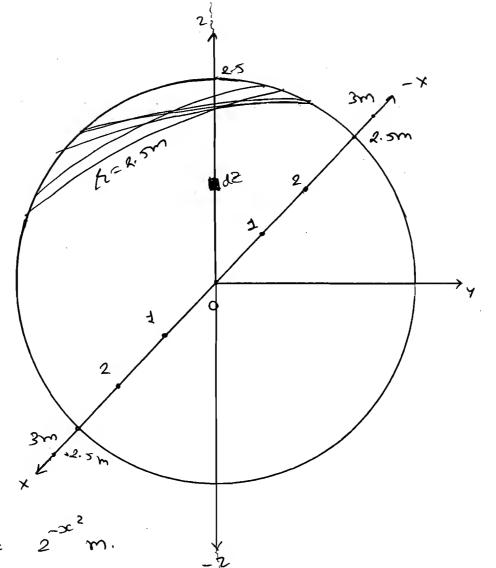
Ex-1 What net electric trux passes through a sphere of Judins dism centered at the origin. Viven the Charge Configuration.

(1) point charges of $a = 2^{2^2} nc$. Which are located at on the x-axis at x=0, ±1, ±2, ±3 m

(2) An infinite line with a unitern Charge density of $1/22+1=\frac{1}{22+1}$ nc/m lies along z-axis.

Ans: 2-38MC

- (3) A Dim unitedim surface charge density of 1 x2 +y2+4 nc/m2. lies in z=0 plane. Ans: 2.95 nc.
- (4) Unitedm charge density 20nc/m, Ries in Z=0 plane and are located at }=0,±1,±2,±3 m. Ans: 403 nc.



x= ±3m are not enclosed > The Charges at

(3)

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by the Sphere

Pret = aenc.

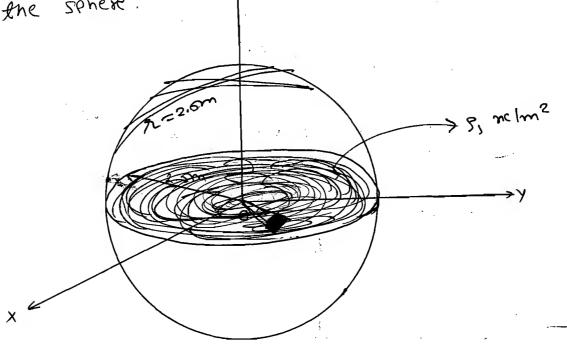
: Ymer = to + 1 + to + =

Yne+ = 2,125 nc.

Part of the infinite line is enclosed by sphere. (2) For 121 \le 2.5 (OR) - 2.5 \le 7 \le 2.5.

do= Sedz. : Ynet = Gonc.

: Oemc = 2.38 nc



> Sphere encloses a circular disk of radius 2.5m Centered at origin and it located in z=0 plane.

here, $9 \le 2.5 \, \text{m}$; 7=0

Put $x = 9\cos \emptyset$, $y = 9\sin \emptyset$

& ds = 8 ds d8

(2)

: da = 9, ds

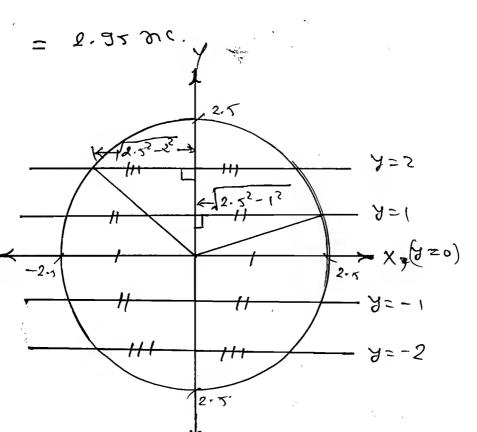
: Prick = Genclosed

$$= \int d \emptyset$$

 $\frac{2\pi}{2} \int \frac{9 \, d9 \, d8}{(5^2+4)}$

 $= \frac{1}{2} \left[\ln (5^2 + 4) \right]^{2.5} \times [8]^{2.5}$

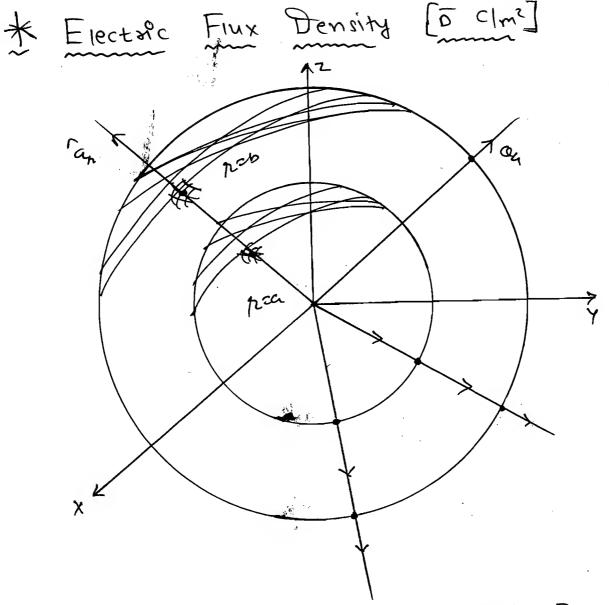
0



 \rightarrow Qnet = Qenc. = $20 \times 10^{9} \left[4 \sqrt{2.5^2 - 2^2} + 4 \sqrt{2.5^2 - 1^2} \right] + 5 \times 20 \times 10^{9}$

= 403 mc.

67



-> Flux per unit Area = Electric Finx Density

Ynet = Qenc = a

Surfure asen of Spriese = 4Th

: Flux Density = a clm2.

Through 1=b.

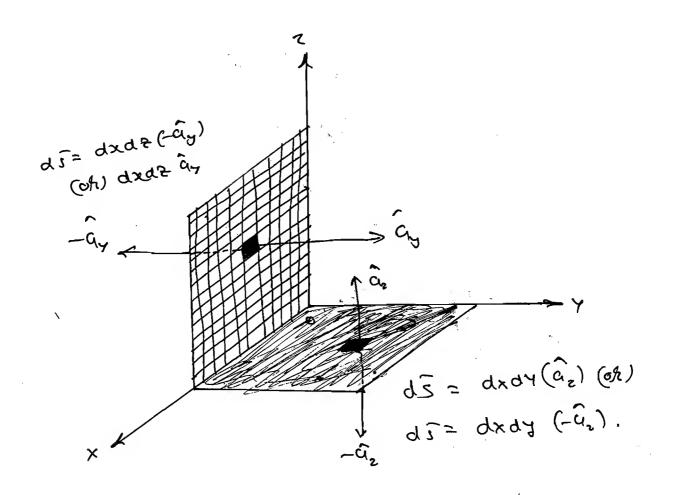
Finx density = atts? (/m2.

magnitude of the blux In general, the density through sphere of rudius 18'm IDI= ame Cloma the hux density is changing Shown, its vaine along radial disection (his) .. we write D= anx2 Gn. E due to a' located at the origin is given by

D= EE

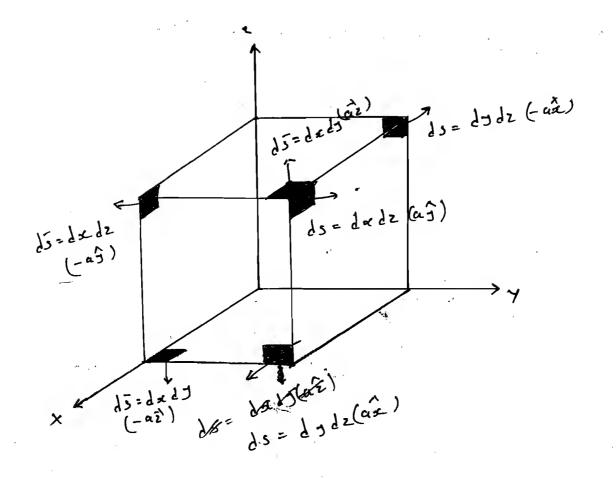
(allulation of D and for the Procedu re Sume. identically are

*> Case-1: Open plume (or) open symbule.



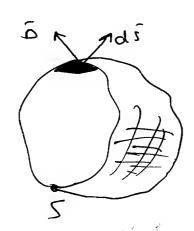
The Vector dibrevention surfue element di of any point on the open plane would be projecting normal to the surface.

 $\frac{1}{\sqrt{3}} = \frac{1}{\sqrt{3}} = \frac{1$



Syrbace any point on the CIOSEd At somer for ord ward Projecting be CONID гb Syggace. the

Craussa Law: form of Integreu



as assitury closed Enstace (2) Shows > Figure d5 would on this sufface end. bount. & Ine noma projecting outward be surface

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enclosing some charge configuration. Somehow we have calculated D at any point on the closed surface

toh e.g. o makes an angre of with di

on the closed surface will their depends upon the Charere Contiguration within the closed surface. whereas direction of ds at any point on the Closed surface would be projecting outward normal to the surface.

) d making any possible value beth of

The differential amount of Mux passing through dī i.e. In a direction normal to the Surface at that point is the projection of on to the dī.

-> Mathematicary,

 $d\varphi = |\hat{a}| \cdot |\alpha \hat{i}| \cos \alpha.$ $= \hat{a} \cdot \alpha \hat{i} \quad \text{if } \alpha$

if x=0 or 180 max. amount of thex passes through ds

7) It K= 90', zero frak Pusses Anrongon de

-> We write aquis levois Intgra form,

→ We assume that the crosed systeme is encrosing a volume charge density of Su cim².

$$\therefore \int_{S} \overline{D} \cdot d\overline{s} = \int_{S} Sudu. - 0$$

Now, using Divergence theorem.

Company (1 20

-> This is a point form of Granss Law.

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(a)

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$$\rightarrow \nabla \cdot \bar{o} = \frac{1}{92} \frac{3}{3n} (92) + \frac{1}{85in0} \frac{3}{30} (sino 0a).$$

$$+ \frac{1}{85in0} \frac{300}{89}.$$

Ex-1 In a region the electric blux density is given by $\overline{D} = (2 \times \hat{a}_x + 3y \hat{a}_y - k \times \hat{a}_e)$ c/m². assume therefore the region then find the value of k.

Ans: Charge free region Su=0

$$-kz = 5 clm^2$$

Ex-2 The magnitude of the Electric trux density is proportional to or where kis constant.

92-> spherical coordinate. The D is projecting in the radical direction. Choose the value of k such that electric trux density has zero divergence.

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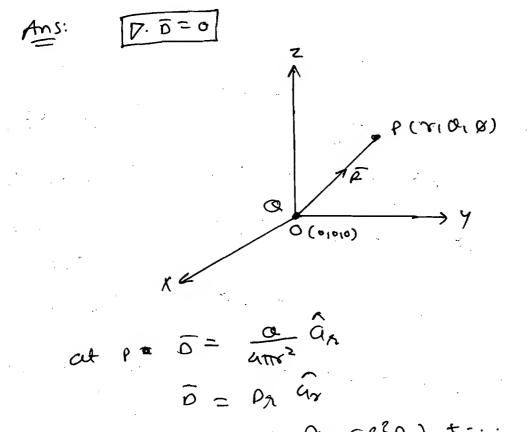
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Ans: Co

(D) & 2K

V.0= 0.

: 1 92 × C19k



$$\nabla \cdot \overline{0} = \frac{1}{92} \frac{\partial}{\partial x} (x^2 o_r) + \dots \\
= \frac{1}{92} \frac{\partial}{\partial x} (x^2 o_r) + \dots \\
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= \frac{1}{92} \frac{\partial}{\partial x} (x^2 o_r) + \dots$$

Ex-4 Let D= (4x392 + x22 9y + exy 2) nc/m2 OSX, y, Z SI. Find the amount of \$4 passing through closed surfuce defined by 0 \ x, y, z \land also find the amount of charge enclosed within it. also indicate weitness the flux enterind a close surrule or

Pret = \$ 5. dJ = \$ 30 dos . = arciosed.

: Oerc = 12x /2] [4], [7],

$$= \frac{12}{3}$$

$$\therefore \boxed{Q_{enc} = 4 \text{ nc.}}$$

Ex- Σ Let, $\bar{D} = 12x^2yz\hat{a}_x + 2xy\hat{a}_y + 3x^2z\hat{a}_z \frac{nc}{m^2}$. find the amount ob Electric blux passing Ansongn a surface define by x=1, 0 57,252.

Ans: $\overline{D} = \frac{12x^2y^2}{4x^2} + 2xy^2 + 3x^2 + 6x^2$ ax disection.

d5= dydz Gx :. O= | | 1272 dyd2. D. 05 = 12 x272. = 12 [42] [22] Cut 20=1 D. d = 1283.

= 12 x K x 9 : [Qenc = 4 x nc]

: | Prez = Oenc = 48 nc]

 $E_{\underline{x}}$ - \underline{G} Let $D = \frac{\pi}{3} \hat{q}_{R}$ $nc|_{m^{2}}$ where π is a Sprenca Co-ordinat, û is a ranit vector in the rudia direction. find Su., amount or electric = hux passing through a sphere of quains Im. Centered at the origin. also indicate
the electric knux rearing the surfaceon entring
Ans: So = 0, 0

$$S_{V} = \frac{1}{92} \frac{3}{38} (x^{2}, 0x).$$

$$= \frac{1}{92} \frac{3}{38} (x^{2}, \frac{9}{3}).$$

$$= \frac{3}{3} \frac{x^{2}}{3}$$

$$= \frac{3}{3} \frac{x^{2}}{3}$$

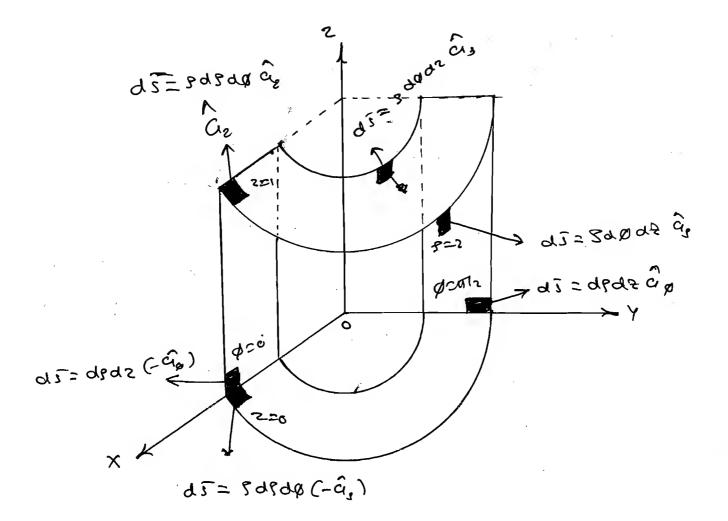
$$= \frac{1}{3} \frac{3}{3} \frac{x^{2}}{3}$$

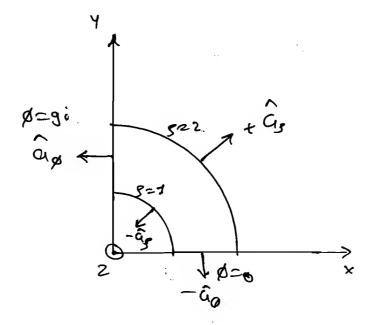
2 =1 m

$$= \frac{1}{3} \left[2\pi \right] \left[-\frac{1}{6} \right] 0,$$

$$= \frac{1}{3} \times 2\pi \times 2$$

$$= \frac{1}{3}$$





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* Mosk:

-> Work is defined as a force acting over distance.

Nork done in moving a charge of a common toom an initial point to the binal point in the vicinity of electric final point in the vicinity of electric field is given by

W= $- O \int \overline{E} \cdot d\overline{z}$ Junies.

Ex-! find a w.o. in moving a 5 lic Charge from the origin to (2,7,4)m through the bield $(2xy^2 \hat{a}_x + x^2 z \hat{a}_y + x^2 y \hat{a}_z)$ V/m. the field $(2xy^2 \hat{a}_x + x^2 z \hat{a}_y + x^2 y \hat{a}_z)$ via the path (0,0,0) to (2,0,0) to (2,-1,0) to (2,-1,4).

Ans: $d\hat{x} = dx \hat{q}_x + dy \hat{q}_y + dz \hat{q}_z$.

 $\overline{F}.d\overline{z} = 2xyzdx + x^2zdz + x^2zdz.$

W.O. = -a | exyzdx + xt2dy + x2ydz.
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 $= -a[L+I+I_3]$ $= -5xi^{-1}[-1c]$

: W-D. = 80 MJ

Ex: ? Repeate the celoure example because the Path x=-24, 7=2x. Ans: de= dxâse + dy ûy + dzâz. (0,0,0) to c 2, -1, 4). $\therefore \widehat{E} \cdot d\widehat{z} = 2xyz dx + x^2z dy + x^2y dz.$ W = -0 \ \(\in \text{E-di} = -5\text{X1.6} \) \(\in \text{Xy2.dx} + \in \text{x2y2} \) \(\text{x2y2} \) $= \sqrt{5} \times 10^{3} \left(\frac{2}{3} \right)^{2} \times 3 \times 4 = \frac{1}{3} = \frac{2}{3} \times 3 \times 4 = \frac{2}{3} \times$ = -5 x1068 -27 to] - [1] - [1]. = /5 x 10 (8 + 1 + 2 16). $W = -5 \times 10^{6} \left[2 \int_{0}^{2} -x^{3} dx + \int_{0}^{4} 8y^{3} dy + \int_{0}^{4} -\frac{z^{3}}{8} dz \right].$: W= -5x1.06 [-1 + 2 - 648] = - 5x1 = 6 [-6 - 1/8].

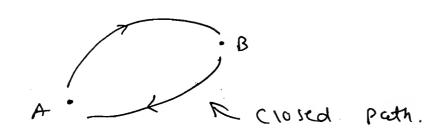
W = 49x5 X10 J.

. پسر (x114'51) to (x5'41'55).

(x, x) to (x2, 2) (x, 2), (x2, 2),

$$\frac{y-x_1}{y-x_1} = \frac{x-y_1}{x_2-x_1} = \frac{x-x_1}{x_2-x_1} = \frac{x-x_1}{x_2-x_1}.$$

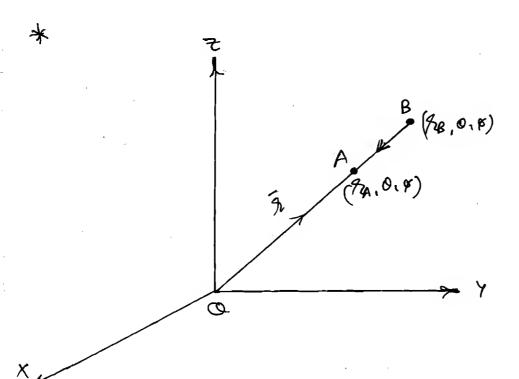
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$$\rightarrow W = -Q \int_{B} \overline{E} \cdot d\overline{z} \int$$

Que define the potential at it with ref.



$$\rightarrow$$
 $\widehat{E} = \frac{O}{4\pi\epsilon R^2} \widehat{Q}_R$

From B to A dg = dg an.

Ry

Theo,

In general

Vp is the Potential Cot P due to 'O'. IFI is the distance blow the charge 'o' and the observation point 'P'.

C=0 if the set. Por (housen at infinity.

0

* Potential Function:

$$\rightarrow$$
 Potentials is a functions of space $(o-ordinates)$ $V(x,y,z)$ (oR) $V(y,y,z)$ (oR)

V(9,0,0).

* Recasion blu postentica condient una Electric fiera: 87

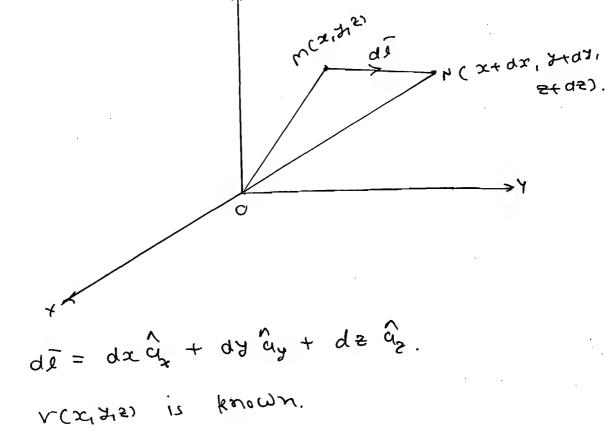
→ We assume that two neigh bourhood points

M, N because of Some charge Configuration

We have known the potential function

V(x, y, z).

is different from potential at N and there exist a potential airberence of dv voits.



(1) $dV = \frac{\partial V}{\partial x} dx + \frac{\partial V}{\partial y} dy + \frac{\partial V}{\partial t} dz$.

->(1)

· We intoudure P (on) Ber (on) brudient operator

-> Croudient Of squar function in vector.

3 PV = 30 00 + 30 Gy + 30 Gy.

@ interms OF 0 20. dv= TV. di - 6 -: V= - \ E- d\(\overline{\pi}

: dv = - B.dj. - 0

From G 2 1

- E.di = VV.di.

suppressing di on both sides.

E= - TV.

- (I) Electric field is the gondient of the scarcer electric potential bunctions.
 - (II) (a) From en-1 we can conclude that electric field projects normal to an equipostrutia system

 \bigcirc

- (B) E would pe benject from a vidues bostentier Syrface to towards lower potential syrface.
- * Egnipotential systuce: -> It is that systeme on which the potential
 - difference bet any two points is 0'-
 - -) we assume that the point m and n lies 001 canipotential surface.
 - (From egn 4 we can conclude that Potentia can vary its vame normal to an

equipotential surfure.

 $\frac{1}{3}\nabla V = \frac{\partial V}{\partial x} \hat{a}_{xx} + \frac{\partial V}{\partial y} \hat{q}_{y} + \frac{\partial V}{\partial z} \hat{a}_{z}. \rightarrow V(x, y, z)$ $\rightarrow \nabla \cdot \mathbf{V} = \frac{\partial \mathbf{V}}{\partial \mathbf{S}} \hat{\mathbf{q}}_{\mathbf{S}} + \frac{1}{3} \frac{\partial \mathbf{V}}{\partial \mathbf{S}} \hat{\mathbf{q}}_{\mathbf{S}} + \frac{\partial \mathbf{V}}{\partial \mathbf{Z}} \hat{\mathbf{q}}_{\mathbf{Z}} - \mathbf{V}(\mathbf{S}_{\mathbf{I}} \mathbf{P}_{\mathbf{I}} \mathbf{Z})$ -> D.V = $\frac{\partial V}{\partial R} \hat{q}_{R} + \frac{1}{2} \frac{\partial V}{\partial Q} \hat{q}_{a} + \frac{1}{2} \frac{\partial V}{\partial Q} \hat{q}_{a}$ certain region the potential field distribution is given by lenzion Jz voits Ohere, & is spnesical consainates assyme medium to be free space. Find E, O. & amount of him. passing through a Ut ruding 5m. centered at origin. also indicate charge enclosed and also indicate the HMX lenving the surbace.

No V (8)= 100 (92) 2

Surbace. : E= - V. V

$$E = -\nabla \cdot \nabla$$

$$= -\frac{d}{dx} \left(100 \right)^{\frac{1}{2}}.$$

$$= -100 \times \int_{a}^{a} \hat{q}_{h}$$

: 0= j g, d0

$$\frac{1}{2} = \frac{1}{2} = \frac{1$$

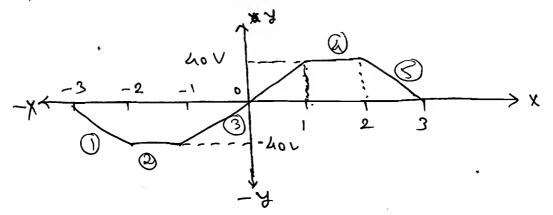
$$= -50 \, 60 \, (5)^{312} \int_{0}^{312} \int_{0}^{312} \sin \theta \, d\theta \, d\theta$$

$$= -50 \, 60 \, (5)^{312} (407) \, C$$

$$\text{Thet} = \text{Qenc} = -50 \, 60 \, (5)^{312} (407) \, C$$

 $(\widehat{\cdot})$

Thet = went -- ψ' is entering to the closed surface. Ex-2 In certain region the potential Great x. 91 distribution is given by the tomowing sketch plat the corresponding electric field.



Ans: $-x \xrightarrow{-3 -2 -1} \xrightarrow{0}$

$$Seg-3 = -1 < x < 1.$$

$$Seg-3 = -1 < x < 1.$$

$$(-1, -40), (1, 40)$$

$$V(x) = -40$$

$$Ex = -4x = 0$$

$$V(x) + h0 = 40 (x + 1).$$

 $E_{x} = -\frac{8}{8} / 8x.$

Ex= -40. V/m

* Dipole:

$$\frac{1}{2} + 0$$

$$\frac{1}{2} = \frac{1}{2}$$

$$\frac{1}{2} + 0$$

$$\frac{1}{2} = \frac{1}{2} + 0$$

93

Ans:
$$\overline{E} = -P \cdot V$$

$$: \overline{E} = -\frac{\partial Y}{\partial \lambda} \hat{q}_{\chi} - \frac{\partial V}{\partial \alpha} \hat{q}_{\alpha}.$$

So, far the quantities E, ψ , D e V have been analyzed. From the lenowiedge of given Charge Consignation there are no procedure available for the measurement of this Charge Consignation but there are procedures available for the measurement of potentials at the given points.

-> From the known potentials it are are able to develope potential bunction i.e. V(x, J, Z) or V(S, &, Z) or V(S, &, Z) or V(S, &, Z)

Poissions and Lapracian's Egn.

(Homo Fening medium).

$$\therefore \nabla \cdot \overline{F} = \frac{g_u}{G}.$$

in a region of intrent it
$$Su = 0$$

then $\nabla^2 V = 0$. Laplacian ean.

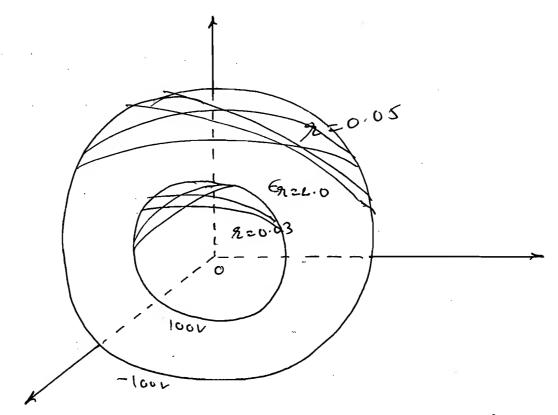
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> For analysing junction Characterstics of a ph diode one dimensional possions ears is used because junction hay a charge i.e. it is an ionic region.

Ex-1 Two concentric Conducting Spheres 93 having sadif 3 cm and 5 cm are Centered at origin. The potential on the Sphere is 100 V - while the inner order sphere is yet - 100V? The region bet Them is villed with a homogeneing. dielectoic having & relative permitity 2-0. pind

- potential bunction.
- 2) potential mid way beth the conducting
- The raine of 2 at which V=0. @ Find the expression for electric field.



as shown in figure, these exists equipotential Systemes at 92= constant we know that potentica varies norma to anogn Quipotratica surface.

Therefore, Potential 5^n must be a 2 alone. Since 8v is not mention bet n the sphere. We assume 8v=0. Therefore, Laplacian ear reduces to $V^2V^2=0$

Cross mutiply and intigres,

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$$\frac{dV}{dh} = \frac{C_1}{R^2}.$$

$$\therefore \quad V = -\frac{C_1}{92} + C_2.$$

$$V (at R= 0.03) = 100 = -\frac{C_1}{0.03} + C_2.$$

solve a and Cz.

(1)
$$\sqrt{(2)} = \left(\frac{15}{2} - 400\right)^{1/2}$$

(3)
$$0 = \frac{15}{\pi} - 40^{\circ}$$

$$(4) \quad \widehat{F} = -\nabla \cdot V.$$

$$= -\frac{8x}{8x} \hat{q}_n$$

$$: \vec{E} = + \frac{15}{92} \hat{q}_{R}. \text{ V/m}.$$

-> The Obtained F is projecting along 9/2 direction and it is projecting town a higher potential surface to towards hower potential.

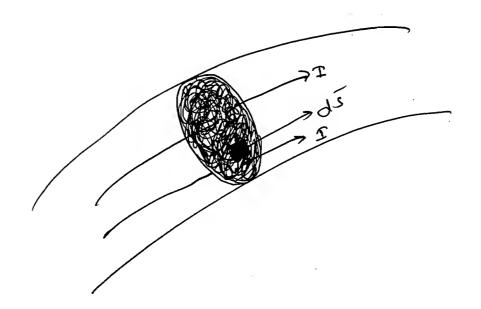
J.: Conduction current Density (Alm2)

Be: Volume Charge density (c1m3).

of = conductivity (v/m).

Ud: dott velocity (m/s).

E = Applied Electric Field.



- -> Across, S', we now the Conduction current density (To Alme)
- -> The diff. amount of current di Passing length dis is given by

 $dI = \overline{J}_c \cdot d\overline{J}$

Ex-1 In Certain region the Conduction arment density is given by -105 DV Alm2 where $V=10e^{2}\sin y$ voits. Scarcer electric potential function. Find [Orductivity of medium.

@ Amount of current pussing through x21, 057,51 in \hat{G}_x direction.

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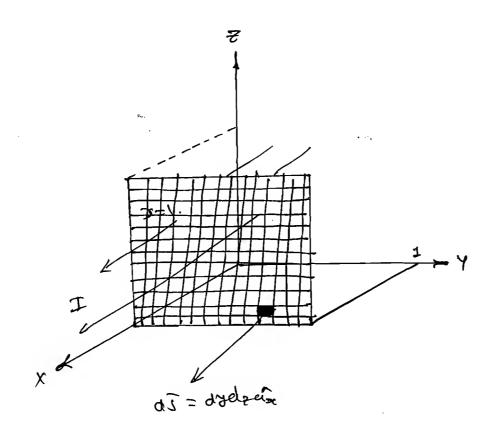
Ans:
$$0$$
 $\overline{J}_c = \overline{C}$.

 $\overline{J}_c = \overline{C} \cdot \overline{C} \cdot$

$$\Theta \qquad \nabla V = \frac{\partial V}{\partial x} \hat{q}_x + \frac{\partial V}{\partial y} \hat{q}_y.$$

$$\nabla V = (-10e^{-x} \text{ sind } \hat{Q}_{x} + 10e^{-x} \text{ cosy } \hat{Q}_{y})$$

 $\therefore \bar{J}_{c} = 10e^{-x} \text{ sind } \hat{Q}_{x} - 10e^{-x} \text{ cosy } \hat{Q}_{y}.$



$$T = \int_{0}^{\infty} \int_{0}^{\infty} dx = \int_{0}^{\infty} \int_{0}$$

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$$\frac{d}{dx} = \frac{d}{dx} = \frac{d}{dx} = \frac{d}{dx} \int_{\mathcal{L}} g_{x} dx.$$

$$(oh) \qquad \begin{cases} \int \overline{J}_{c} \cdot d\overline{S} = -\frac{2}{24} \int SudV. -0 \end{cases}$$

Using divergence Incorem.

point form.

: m+ = =0

== C₁e = t/z == C₁e = t/z

Z= Relaxation time.

-> we concinde that as the time progresses the charge density inside a conductor decays exponetially. The rate at which it decays exponetiany depends upon Conductivity the Conductor. It a conductor having insinite conductivity the density inside a conductor tends to zero within no sime. In other words, for a trunsient fine they muy be some non zero charge inside a conductor.

-> Further we can conclude that it any Charge is present in any conducion it resides on the surface of the conductor 0817.

Find the relaxation time for a copper Ex-1 conductor whose conductivity is sometime assume E= Fo. also find % or charge density after I relaxation time and after 5 relaxation time. T= Eo. C= 8.82 X10 7= 1.6 x10 13 5. Se (at t=z) = c(e = = c/e = 0.36c, Pu (ce t=z) = 36.1.06 C1. -52(2 = cles = 0.00679. Pe (at t= 57) = 9€ Se (Cet t=52) = 0-67-1. 07 C1. -t/2

0-36C1

0.00679

t=0

.)

 \odot

* Boundary Conditions: * case-1: Conductor interface. (09) Conductor to dienectric interfuce. -> An interface is a plane like Stancture onere two mediums are interacting, In this case we assume conductor interface (or) Conductor to digrector interfuce. We have to investigate behaviour of electric bield and electric flux density across the interface. Interbuce -> an: Normal unit vector directed from conductor to dierectoic. -> \hat{G}_{k} : Unit vector tungential to the Interface. \$ E.dē =0.

 $= \sum_{i=1}^{n} \widehat{E} \cdot d\widehat{I} + \sum_{i=1}^{n} \widehat{E} \cdot d\widehat{I} + \sum_{i=1}^{n} \widehat{E} \cdot d\widehat{I} + \sum_{i=1}^{n} \widehat{E} \cdot d\widehat{I} = 0.$

-> The I has to be Computed inside a conductor.

-> The charge is zero inside a conductor. Therefore, Electric field is zero inside a ()Conductor and hence this integrow vinishes. \cdot (\cdot) -> we use interested to investigate behaviour \bigcirc of electric field across interface. So to \bigcirc \bigcirc accomplishe this we choose path like 1-2 and 3-4 so small such that the path 2-3 is gruzing the interfuce, Which would (fonching) result the I and I vanishing. (E.d. = 0. \rightarrow For Poeth (2-3) => de = de cu Let F = Enant Et 92 This is assumed across the interfuce. : E-dé = En. an. de ât + Et ût. de ât : F.de = Fedl ⇒ \ Eq. df = 0. : de camt be ZERO. : Etco -> Tangential Components of electric field almost Kanishing. a Conductor to diffection in tensuce

Across a Conductor Interface identity 165 the correct one from the following: where \bar{E} is the electric field across the interface \hat{a}_{k} : unit vector temperative to Interface. \hat{a}_{n} : the unit vector mornal to Interface.

(i) \bar{E} : $\hat{a}_{k} = 0$ (v) \bar{D} : $\hat{a}_{n} = s$:

(ii) \bar{E} × $\hat{a}_{n} = 0$ (vi) \bar{a}_{n} . $\bar{b} = s$.

(iii) \hat{q}_{n} × $\bar{E} = 0$.

(iv) An the above.

De assume that the Interface hay a non-zero surface charge density ob

So and By using Crauss Law we can shaw that normal components of Electric flux densities are equals to surface charge density. By expression

 $D_{n}=S_{s}$ (of)

D= Ss an and

The entire charge ises

on the top of the conductor

surface.

on both sides U6 Conductors Sheet.

Ex-1 A Charge density of 1 nc/m² is placed on a conductor surface. Assume interface is free Space. Find the magnitude of the exceptic field.

Ans:
$$\overline{E} = \frac{S_1 \, \widehat{q}_n}{E} = \frac{1 \times 10^{-9}}{3 \cdot 17} \, \widehat{q}_n$$

Ex = A Positive Charge is distributed on a conductor surface. Assume the Interface is force space. When that D at across interface is equal to D= 2 (ax + J3 ay) norms.

find the value of charge density across the interface.

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w'()

$$\widehat{E} = \frac{g_1}{e} \widehat{q}_n.$$

$$\widehat{a}_m = \frac{g_2}{g_3} + 2\sqrt{3} \widehat{q}_3$$

$$\widehat{b} = \frac{g_3}{f_4 + 12}$$

$$\widehat{a}_n = \frac{\widehat{a}_{34}}{f_4 + \sqrt{3}} + \frac{\sqrt{3}}{2} \widehat{q}_3.$$

$$|\vec{D}| = \sqrt{\frac{2^{2} + 2^{2}(3)}{4}} = 4.$$

$$|\vec{D}| = \sqrt{\frac{2^{2} + 2^{2}(3)}{4}} = 4.$$

: 3/2 4 nc/m2.

Case-2: Diesectoic to Diesectoic intertace: medium (2) â

an: Mormal unit vector directed in som Otop Qu: Tem Unit vector tungentien to the Interfuce.

We can show that

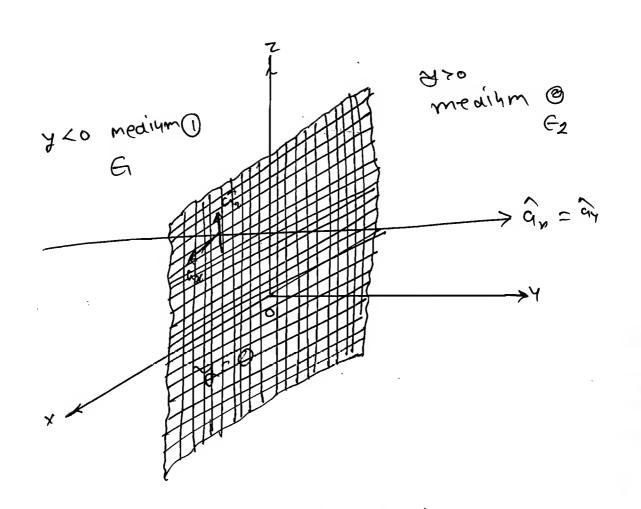
Tangentier Components of E-fields are confirmens across a diectric to diectric interface.

(2) (a) [Dn2 - Dn1 = 35

- The normal components of electric fine densities are dis continèred by an amount of surfue Charge density.

(b) it Ss=0 (charge tree interface).

-> The normal components at electric trux densities are continenemy across a churge bee interfuce.



-> bigure snows that interfuce is define by some y=0. Medium -1 is define d'for y <0 and is characterised by \(\xi_1 \).

The unit vectors tungential to interface are \hat{a}_{x} and \hat{a}_{z}

Exit with reference to the figure shown above Let, $\epsilon_1 = 2 \epsilon_0$, $\epsilon_2 = 3 \epsilon_0$. and given that $\overline{E}_1 = (4 \hat{a}_x^2 + 5 \hat{a}_y^2 + 6 \hat{a}_z^2) \text{ V/m}$.

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Find Di 1 DZ 1 & and Ez. and assume there's the interface is charge bree: (it) Ss=0 () across $\overline{E}_{i} = \frac{4\hat{a}_{x} + 6\hat{u}_{y}}{E_{h}} + 5\hat{u}_{y}$ \overline{E}_{h} \overline{E}_{h} : E = Exi az + Eni an -> (i.e) Any field vector across the interfuce Con se represented as a vectorial sum ob tungential and normal components. $\overline{E}_{i} = 4\hat{a}_{i} + 6\hat{a}_{i} + 5\hat{a}_{i}.$ 01= E1 f1 $= \lambda \in \hat{\alpha}_{x} + 6 \in \hat{\alpha}_{y} + 5 \in \hat{\alpha}_{y}$ Et = Etz $\overline{E_1} = u \hat{q}_{11} + 6 \hat{q}_2 + F_{y_1} \hat{q}_y$ == Dn1 = Dn2 (= 5, =0. Dz = Dx2 Qx + Dz2 Qz + 56, Qy.

 $D_{2} = D_{X12} \hat{\alpha}_{x} + D_{22} \hat{\alpha}_{z} + 5 \hat{\alpha}_{x} \hat{\alpha}_{y}.$ $D_{2} = C_{2} E_{2}$ $D_{XL} \hat{\alpha}_{x} + D_{22} \hat{\alpha}_{z} + 5 \hat{\alpha}_{z} \hat{\alpha}_{y} = 4 E_{2} \hat{\alpha}_{x} + 6 E_{2} \hat{\alpha}_{z}$ $D_{XL} \hat{\alpha}_{x} + D_{22} \hat{\alpha}_{z} + 5 \hat{\alpha}_{z} \hat{\alpha}_{y} = 4 E_{2} \hat{\alpha}_{x} + 6 E_{2} \hat{\alpha}_{z}$ $D_{2} = 4 E_{2} C |m^{2}|$ $D_{3} = 4 E_{2} C |m^{2}|$ $D_{3} = 6 E_{2} C |m^{2}|$ $D_{3} = 6 E_{2} C |m^{2}|$

II.

Ex- ? Repeat the above problem it the interface has a non-zero surface charge density Ps clme let, $\overline{D_2} = Dx_2 \hat{\alpha}_x + Dz_2 \hat{\alpha}_z + Dy_2 \hat{\alpha}_z$.. Dne- Dn1 = 95 DAS - DA = 37 .. Dyz = 9, + = 5G. D2= Dx2 ax + D22 a2 + (9, + 56,) ay. Dz = Ez Ez DXZ= GEZ Clm? \odot D22 = 6 Ez Clm?. ٩ ... Eyz = 8, + 54 V/m. \odot 9 Ex-3 Repeat above 2 example by assuming (-- the Interface as ZEO. ZEO is medium I and is characterized by EI whereas Z>O is medium 2 una is characterized 0 by E2. $\overline{E} = \frac{4 \hat{\alpha}_{xc} + 5 \hat{\alpha}_{y} + 6 \hat{\alpha}_{z}}{\overline{E} + \overline{E} + \overline$ \bigcirc $\frac{\widehat{E}_{n}}{\widehat{E}_{n}} = \widehat{E}_{n}$

is directed in form medium I to e. is unit vector 1 az. 8 unit vector tungenties le interfuce are and ay. FE2= Et1 = Ftz + Enc. Dn2 = Dn1. $\vdots \quad \in_{\epsilon} \widehat{E}_{n_2} = \quad \in_{\epsilon} \widehat{E}_{n_1}.$ $= \overline{E}_{n_2} = \frac{\epsilon_1}{\epsilon_2} \overline{E}_{n_1}.$ $\frac{1}{16} = \frac{2}{3} \times 6 \hat{\alpha}_{2} = 4 \hat{\alpha}_{2}.$ $= \left| \overline{E}_{2} = \mu \hat{a}_{x} + 5 \hat{a}_{y} + \mu \hat{a}_{z} \right|$ $\widehat{D}_1 = \epsilon_1 \widehat{E}_1$ | D̄1 = €0 (8û), + 10û, + 12û2) $\overline{D}_2 = E_2 \overline{E}_2$ $\sqrt{p_2} = 606 12 \hat{q}_x + 15 \hat{q}_y + 12 \hat{q}_z$). Mom! these is are sussainer combonents of D that are discomined by surface charge density so c/m2. Dn2 - Dn, = 3, c/m2. -: E Enz - E Enz = Ss.

• :

$$E_{2} = \sum_{i=1}^{n} \frac{1}{E_{1}} = \frac{E_{1} E_{1} + S_{3}}{E_{2}}$$

$$E_{1} = \frac{E_{1} E_{1} + S_{3}}{E_{2}}$$

$$E_{2} = \frac{E_{1} E_{1} + S_{3}}{E_{2}}$$

$$E_{2} = \frac{E_{1} E_{1} + S_{3}}{E_{2}}$$

$$E_{3} = \frac{E_{1} E_{1} + S_{3}}{E_{2}}$$

$$E_{4} = \frac{E_{1} E_{1} + S_{3}}{E_{2}}$$

$$E_{5} = \frac{E_{1} E_{1} + S_{3}}{E_{2}}$$

$$E_{7} = \frac{E_{1} E_{1} + E_{2}}{E_{2}}$$

$$E_{7} = \frac{E_{1} E_$$

$$\overline{D_1} = \epsilon_0 \left(8\hat{\alpha}_x + 10\hat{\alpha}_y + 12\hat{\alpha}_c \right).$$

medium e, O Interface ((harge) free). medium E

-> Fig. Shows Charge free diesectric to diesectric interface. Rusquer it is Shown normes unit xector directed in from medium (1) to medium 3 of P. Relate an expression di, de l'Elle.

| Etil= | Etzl. Ans ::

:. Ez (0) (90-d1) = E (0) (90-d1).

:. Ezsindz= Ezsind,

: El Exila Janotez

El stady Elson

Dni - One = Ps

But 8,20

one = one.

? EI |E, | = EZ |Ez1, Co) 4

tint = tint?

Ext An interface is define by 2x+37+42=12 oxigia side of the interface is medium o and is Characterised by E1= 26. Othersiae of the interface is medium - @ and is Characterised by fre space. Lex, the electric field in the medium-1 is given by Fi= 59x + 69y + 702 Vlm. Assume Churge tree interface. Find \overline{D}_1 , \overline{E}_2 , \overline{D}_2 . 2x+3y+42=12. PAS X RBC : = + 4 + 3 = 1. RAS = -69, + 342 PAR X RBCT C 4 (0,4,0) an = -3[402 + cay + $\frac{2}{R_n} = -6\left(2^{\hat{\alpha}_x} + 3\hat{\alpha}_y + u^{\hat{\alpha}_z}\right)$

 $= -\frac{(2\hat{q}_{3c} + 3\hat{q}_{y} + 4\hat{q}_{z})}{8-385}$

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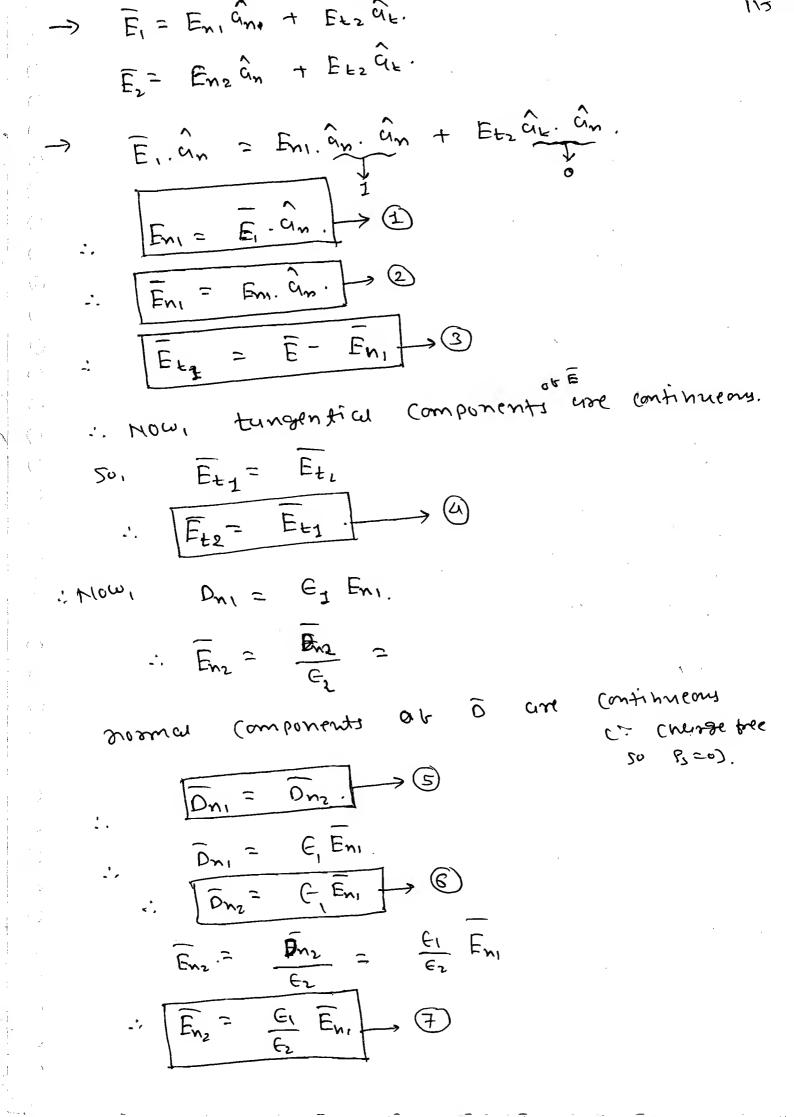
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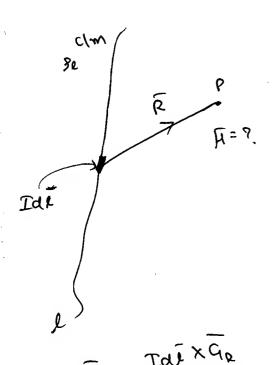


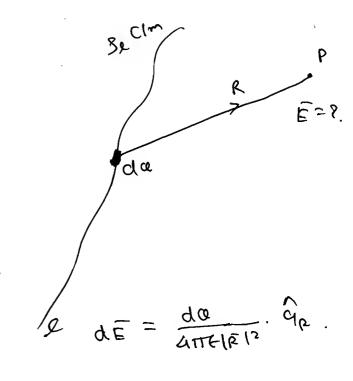
So,
$$E_3 = E_{12} + E_{112}$$
 $E_{11} = E_{12} + E_{112}$
 $E_{12} = E_{12} + E_{112}$
 $E_{11} = E_{12} + E_{112}$
 $E_{12} = E_{12} + E_{112}$
 $E_{11} = E_{12} + E_{112}$
 $E_{12} = E_{12} + E_{12}$
 $E_{12} = E_{12} + E_{12}$
 $E_{13} = E_{12} + E_{12}$
 $E_{14} = E_{12} + E_{12}$
 $E_{15} = E_{15} + E_{15}$
 $E_{15} = E_{15} + E_{$

C

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Fierds R Independent of time.





Current Element = IdI

= Current mutiplied rector dille length

- This is vector quantity. L→ Source of magnetic field.

- -> There exists a similarity bet electric and magnetic fields.
 - -> Both fields are proportional to the Gores ponding

-> Born fierds are inversery Proportional to Square of distinct from their caresbonding Swrces.

fields are kector fields. -> Both => Bio Savart's Law: \ominus Ex-= Find con expression ton the Magnetic field intensity due to a long storight 0 inbinite bilumentay conductor which carries a direct current of I A. Show that the magnetude of the H Musherita intensity. is inversif proportional to the distance been infinite Current filament and the Observation ()point. we assume that the infinite (your oft ()(1) filament lies along z axis. and is extending from - or to too. We find the magnetic field intensity at some

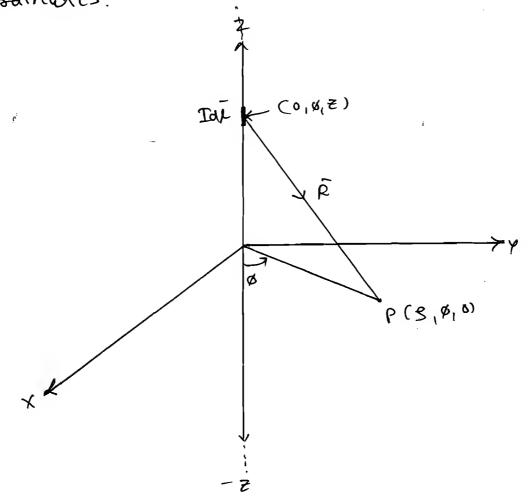
Point on the X-4 Plane.

-> Suy at 9 point P (3, 8,0).

circular (yiiharical ton the convinience we

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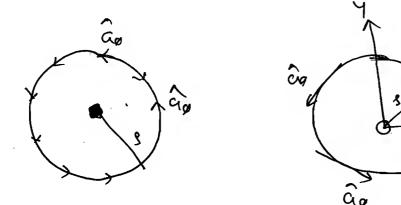
Co-ordinates.



:
$$\overline{H} = \frac{I}{4\pi} \int \frac{9}{(9^2 + 2^2)^{3/2}} d^2 \cdot G_{p}$$

$$\overline{H} = \frac{T}{4\pi} \int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} \frac{g^2 \sec^2 \alpha}{g^3 \sec^3 \alpha} d\alpha = \widehat{\alpha}_0$$

$$= \frac{I}{2\pi g} \cdot \hat{q}_{g}$$



-> Magnitude of magnetic bierd intensity is inversely proportional to the distance bet the infinite current filament and the observation point. The direction of

the Magnetic Field is around the Conductu.

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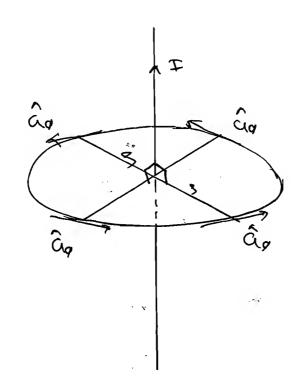
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Two Infinite Current filament use

pasculled: Care-1: Currents care in same direction:

They are separated by 2am. Caro. They

Charles equal current of I amp. In some

airction. Find the magnitude of the

airction. Find the magnitude of the

magnetic field intensity

at the middle point beth this two

infinite (urrent filaments. Assume that

this (orductor's array equal currents of I

comps. in the Same direction.

The fields add in out of phase : |FI| = 0.

0

$$|\overline{H}| = \frac{\overline{T}}{2\pi u} + \frac{\overline{I}}{2\pi u} = \frac{1}{\pi u}$$

The field are add and in phase.

for the Magnetic 123 Expression General Intensity due to an infinite

biament.

P (3, 8,0). (0, ø, 0) 1R1= 9.

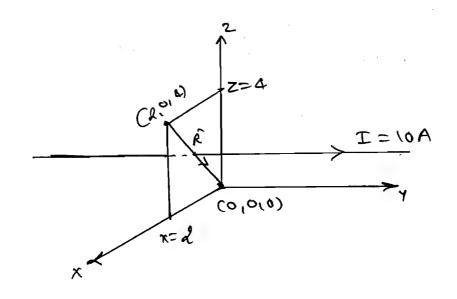
de = de az $\bar{\rho} = S \dot{\alpha}_{s}$. $\hat{\alpha}_{e} = \hat{\alpha}_{s}$

di x âp = âp dz. The unit vector of dixer = dod. Go

I Unit vector ob (di xq̂p).

Short-cut bormucu.

An infinite current frament is lies X=2, 8= 224m it carries a current 06 do A along the of direction. Find To ingino? Ans.



$$= \frac{1}{1} = \frac{-2\hat{q}_x - 4\hat{q}_z}{\sqrt{20}}, \quad \sqrt{1} = \frac{1}{20}$$

$$= \frac{-2\hat{q}_x - 4\hat{q}_z}{\sqrt{20}}.$$

$$\hat{c}_{ig} = \frac{-2\hat{q}_{ig} - \mu\hat{q}_{ig}}{\sqrt{\omega}}, \quad d\bar{z} = d\hat{y}\hat{c}_{ig}$$

$$\overline{H} = \frac{I(\alpha_2 - 2\alpha_3)}{2000}$$
 Alm.

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-> Figure Shows a finite length current filament lies along z-axis. It cames a current of I A.

- Find the Magnetic field Intensity at P (3,8,0). in terms of die de.

-> are know that tak into d Fi = Ids dZ Q. Q.

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: Now, Gos finite length (2, to 22).

: $H = \int \frac{I d^{3} d^{2}}{4\pi (p^{2} + z^{2})^{3/2}} \frac{\hat{G}_{p}}{2}$: $H = \frac{I}{4\pi} \hat{G}_{p} \int \frac{P d^{2}}{(p^{2} + z^{2})} \frac{P d^{2}}{2}$

z = Stan O 5 NS+8 : dt= g secla $\sin 0 = \sqrt{\frac{2}{2^3 + p^2}}$: H = IT Sec20. do Co (010 = N=2+22 Fi = I Sina] 30 Z $\bar{H} = \frac{I}{4\pi l} \left[\frac{2}{(z^2 + \beta^2)^{1/2}} \right]^{22} \hat{C}_0$ Fr = I (22+82)3/2 - N22+82 J. Ca F= I Sind_ Sind_ Co

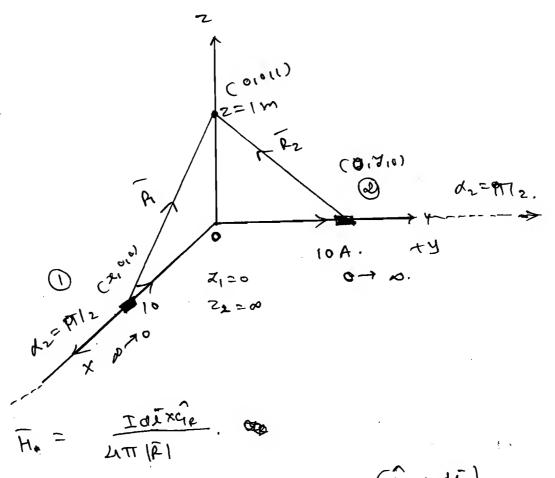
$$\Rightarrow Ib = 2 \rightarrow 0 \Rightarrow 0 = 1 \qquad \Rightarrow Sin I = 1$$

$$\Rightarrow Ib = 2 \rightarrow 0 \Rightarrow 0 = 1 \qquad \Rightarrow Sin I = 1$$

$$\overline{H} = \frac{\overline{I}}{4\pi s} \left[1 - (-1) \right] \hat{Q}_{\emptyset}$$

$$\overline{H} = \frac{\overline{I}}{2\pi s} \hat{Q}_{\emptyset}$$

A Current of top is directed in from 120 infinity towards origin on the positive x-axis and then map to 00 on the cura then and then map to 00 on the tree y-axis find magnitude of magnetic tre y-axis find magnitude of magnetic great intensity on the y-axis. at z=1 m.



$$\frac{d\vec{l}}{d\vec{l}} = dx \hat{\alpha}_{x}$$

$$\frac{d\vec{l}}{dx} = -x \hat{\alpha}_{x} + \hat{\alpha}_{z}$$

$$\frac{dH}{dH} = \frac{T dd}{(y^2+1)^{2}h^2} \hat{G}_{x} - \frac{T dx}{4\pi (x^2+1)^{3}l^2} \hat{G}_{y}.$$

$$\frac{dH}{dH} = \frac{T}{4\pi} \left[\hat{G}_{x} + \hat{G}_{y} \right].$$

$$\frac{dV}{dV} = \frac{1}{4\pi} \left[\hat{G}_{x} + \hat{G}_{y} \right].$$

$$\frac{dV}{dV} = \frac{1}{4\pi} \left[\hat{G}_{x} + \hat{G}_{y} \right].$$

$$\frac{dV}{dV} = \frac{1}{4\pi} \hat{G}_{x} + \hat{G}_{y} \hat{G}_{y}.$$

$$\frac{dV}{dV} = \frac{1}{4\pi} \hat{G}_{x} + \hat{G}_{y} \hat$$

$$Idi = Iado a_{\delta}$$

$$R = -a_{\delta} + b_{\delta} a_{2}$$

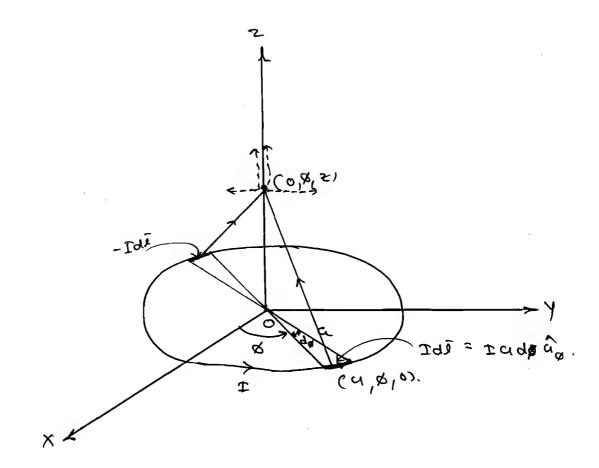
$$G_{e} = \frac{-a_{\delta} + b_{\delta} a_{2}}{a_{2} + b_{\delta}}$$

$$Idi \times a_{\rho}$$

$$= Ia^{2} d \times a_{\rho}$$

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As snown in the figure for every differential Current Flament on the circular around hop. Inese exilt an unather differential current tiloment dimeteracaly opposite side which resurtes in concellation of a nosizontal field Components and the resultant field would be along az disection only. > Ignoring as components the total field

by

is given

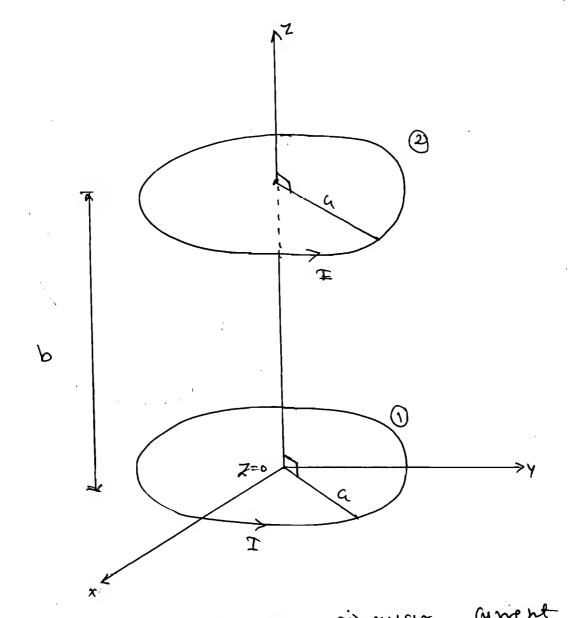
dh = ta2 ant Inbag 41 (a2+62)312

$$H = \frac{\int a^2}{u\pi (a^2 + B^2)^{3/2}} \int_0^a d\theta.$$

$$H = \frac{\int a^2}{2(a^2 + B^2)^{3/2}} \int_0^a d\theta.$$
The centre of the loop (put \$20), the

expression for magnetic field intensity is

*



-> Figure Shows paramed circular ament 100ps

O & @ Find Fi at 2=6 at the centre

ob loop - @.

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$$\overline{h}_2 = \frac{1}{2\alpha} \widehat{a}_2.$$

$$\frac{H = H_1 + H_2}{H} = \left(\frac{\Gamma \alpha^2}{2 (\alpha^2 + \beta^2)^{3/2}} + \frac{\Gamma}{2 \alpha}\right) \hat{Q}_2$$

-> The line Integral of Magnetic bield Intensity around a Closed path is equal to current enclosed by the path.

$$\therefore \ \ \mathcal{I} = \int_{S} \overline{\mathcal{I}}_{c} \cdot d\overline{s} \ .$$

$$\int_{\mathcal{L}} \widehat{\mu} \cdot d\widehat{\rho} = \int_{\mathcal{L}} \widehat{J}_{\mathcal{L}} \cdot d\widehat{\rho}$$

MOW, By Stope's' theosem.

$$\frac{1}{1000} = \frac{1}{1000} = \frac{1$$

crosed puth.

 $\therefore \quad \nabla \times \overline{H} = \overline{T}_c$

point toam of Ampereis Law.

-> The closed path is touching the

the path Ienc=I.

 $\Rightarrow \nabla \times \vec{H} = \begin{vmatrix} \hat{G}_{x} & \hat{G}_{y} & \hat{G}_{z} \\ \frac{\partial}{\partial x} & \frac{\partial}{\partial y} & \frac{\partial}{\partial z} \end{vmatrix}$ $| H_{x} + H_{y} + H_{z} + H_{z$

TXT = 1 Qs Scip ciz 1 8 200 0102 Hs QsHx Hz

TXH = 1 | Qx 9290 Rsino 90 | Ax 9290 Prino 90 | Ax 9100 About Prino Ha

Ex 1 Let,
$$\overline{H} = -Y(x^2+y^2) \hat{Q}_x + x(x^2+y^2) \hat{Q}_y$$
 Alm. 133
Find the amount of another pussing through $Z = 0$, in $-1 \le x \le 1$, $-2 \le y \le 2$ in \hat{Q}_x direction.

$$\nabla x \overline{H} = \begin{bmatrix} \widehat{\alpha}_x & \widehat{\alpha}_y & \widehat{\alpha}_z \\ \partial l_{\infty} & \partial l_{\gamma} & \partial l_{\gamma} \\ -y(x^2 + y^2) & x(x^2 + y^2) & 0 \end{bmatrix}$$

$$\overline{\nabla}_{c} \cdot d\overline{J} = \left(L (x^{2} + y^{2}) \, \widehat{G}_{r} \right) \left(dx dy \, \widehat{G}_{r} \right).$$

$$\overline{\nabla}_{c} \cdot d\overline{J} = \left(L (x^{2} + y^{2}) \, \widehat{G}_{r} \right) \left(dx dy \, \widehat{G}_{r} \right).$$

$$\int_{c^{-}} d\bar{s} = \mu(x^{2} + 0)$$

$$I = \int_{c^{-}} \int_{c^{-}} d\bar{s} = 4 \int_{c^{-}} (x^{2} + y^{2}) dx d\bar{s}.$$

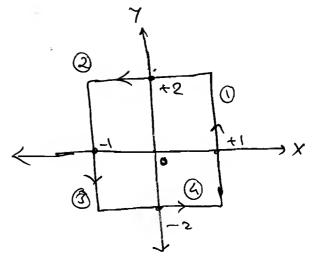
$$= 4 \left[\int_{-2}^{2} x^{2} dxdy + \int_{-1}^{2} y^{2} dxdy \right]$$

$$= 4 \left[\left[\frac{x^3}{3} \right]^{-1} \left[x^3 \right]^{-2} + \left[\frac{y^3}{3} \right]^{-2} \left[x^3 \right]^{-1} \right]$$

$$T = 4\left[\left(\frac{2}{3}\times4\right) + \frac{16}{3}\times2\right].$$

$$=4\left[\frac{8}{3}+\frac{32}{3}\right].$$

-> Method = : by Integral from



-: Path No de Path is at path inde has at $\frac{1}{(1+y^2)}dy$ (1) dyay x=1 $-2 \le y \le 2$ $x(x^2+y^2)dx(1+y^2)dy$

(1 +15 x = -1 - x (x2+x1) y - (1+72) dy

(3) dy = -1 $2 \le y \le -c$ $-1 \le x \le 1 - y(x^2 + y^2) dx = 2(x^2 + 4) dx$

(4) $dx = \frac{2}{3}$ (y) dy = -2 $= \frac{2}{3} + 2 + \frac{8}{3} + 2 + \frac{8}{$

 $\int \bar{\mu} \cdot d\bar{x} = \int -2(x^2 + 4x) dx = 2\left[\frac{x^3}{3} + 4x\right]_{-1}^{1} = \frac{4}{3}, + 16$

 $\int \bar{\mu} d\bar{x} = \int -(1+y^2) d\bar{x} = \left[\frac{y^3+y}{3}+\frac{y}{2}\right]_{-2}^2 = \frac{16}{3} + 4$

 $\int \bar{\mu} \, d\bar{y} = \int 2(x^2/4) = 2 \left[\frac{x^3/3}{3} \right]_{-1}^{1/2} \approx 66$ $= \frac{4}{3} + 66$

$$I = \oint_{A} H \cdot dA$$

$$= \frac{16}{3} + \frac{16}{3} + \frac{4}{3} + \frac{4}{3} \cdot + \frac{40}{3}$$

$$I = \frac{40}{3} \cdot + \frac{40}{3}$$

$$I = \frac{160}{3} A$$

* Application ob Ampere's Lew:

=> For Symmetrical Current distribution where Que have un iden about the direction of magnetic field Intensity then one can find out magnitude of the magnetic field intensity. by using the bollowing procedure.

- -> 1 one has to choose a suitable appropriate crosed path which is enclosing particuly (02) build the given current distribution
 - 2) di always ries arong the path
 - -3 The clusted puth is so choosen in such a any that I may lie along the path or normal to the path
 - P. dZ = [FILGET ib H vics arong the path, H.de = 0 it H normal to the path.
 - (4) over that part of the path where fi lies clong the path, on that part of the Path

H is constant. Ex-1 Find H due to a long stonight intinite ()bilamentary Conductor which Comies () disect current of IA. Que assume that the insinite current filament lies along z axis 0 sdøå, =di. A circular poetre is choosen of 3= const. (200) il (1) $(\overline{\mathbb{Q}})$ Choosen. dē = gdø ûø. 0 ground the > I would be F= Holago Rivo conductor. (3) R-ar = Shodo. (FI = Hø must be Const. on g=const. 4 -: It lies along the path.

Jenc = I (the total (unext 1s enclosed). 137 \therefore $\oint \hat{\mu} \cdot d\hat{i} = \text{Tenc.}$: Ienc = has dø. : I = H, 9 2TT. $\therefore H_{\varnothing} = \frac{1}{2\pi 3}.$: | F = I QNTS Go infinite social Exis kind & que groud come Childrica conductors of sadius a where Current I uniformally distributed gurongmant the coss section. Ans we assume that the solid childranical Conductor possion along z-axis on shown in is the bigure. where the current I is unifarmit distributed throughout the Cross section one am find I for (1) 370 @ g<a. 329

(370) is Choosen.

Q de = adø qø.

3 F= ho ag.

H-de = a Ho do.

(4) (FI) = Hø must be const. on g=const. : Fi is along the path.

Ienc = I (The total (unrent is enclosed).

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 $: \oint \bar{\mu} \cdot d\bar{z} = \text{Tenc.}$

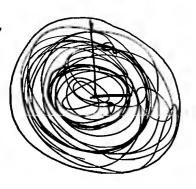
: and Jdx = I.

· attu hø = I.

 $H_{\varphi} = \frac{I}{2\pi\alpha}.$

 $\frac{1}{2\pi u} = \frac{1}{2\pi u} \hat{q}_{g}$

وي اي ع د ٩.



 $TTU^2 \rightarrow I$ $T e^2 \rightarrow I'$

: Ierc= Hes x I

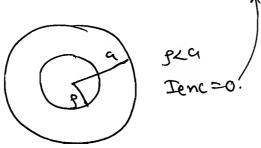
-: Tenc = Ie?

β Fi-de = Ienc => Hø (2π\$) = IPT az.

Ex-2 Repeat the above problem it it is a honor cylindrical Conductor of radius a.

Ans: (i) S > C $\mu = \frac{I}{2\pi s} \hat{G}_{g} = \frac{I}{2\pi s}$

(ii) 924 F=0



Mugnetic Flux Density (B) T (0%) Wb/m2. Unit >> B= MA. h= lote Him. M: Permiability Inductivity (Hlm). Absolute permiability | Inductivity (HIM). ()Ma: Recetive Permiawily or Iductivity Specifies property of a medium and that indicates ability to store the magnetic energy. 3 **(** Charles Street BASA HOSA 600 finx: \$ wb. Magnetic () 1 -> The amount ob magnetic finx passing 141 through a (ross) sectional surface 's' is given by. Ø =) B. ds s Cooss sectional 53= assitury crosed Systace. Ø 53 \$ B. 45 = 0. = \$\forall \tau \cdot $|\nabla \cdot \mathbf{B} = 0$ Cranss Lew for H-fields. -> for electric field Unex = aenc = & Dai = | D. Ddu. G: JV. 0=90 Gauss Gerd for E-Geros.

> Unlike a elector blux the magnetic blux and drot have Starting point and an ending point it enteres the (losed Surface and leaves the same clisted susface as shown above one can find out the amount of magnetic himx Passing through a cooss sectional systace.

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(1)

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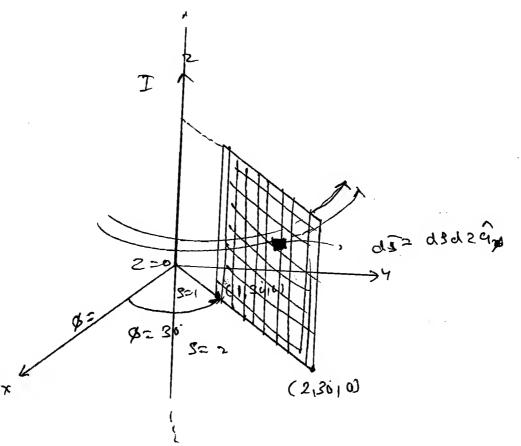
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Ex-1 Find the amount of magnetic Hux. Pusing through a cross-sectional systace define by Ø=30; 15852, 05753. due to an infinite current filyment lies along z-axis. Which corries a direct current of disA aims the 2-direction. Assume ucho.



$$\phi = \int \overline{B} \cdot d\overline{J}$$

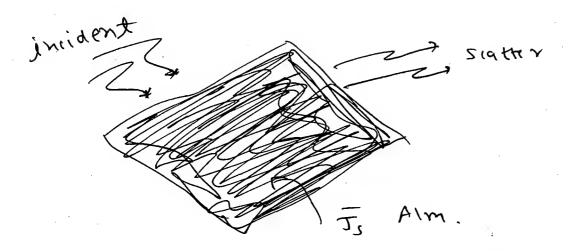
$$= \int \int \frac{h_0 \Sigma}{2\pi S} dS dS.$$

$$Q = \frac{3h_0 \Gamma}{2\pi} \ln 2 \qquad COD$$

`

Boundary Condition: Medium @ M2= Molher M= Logn "Medium O (I) Using Ampères Law, one can show that (a) | Ht = Ht2. Tangential Compnents Of H- fields use continuéay across a worked bee intertuce. (b) $(\overline{H_1} - \overline{H_2}) \times \hat{q}_m = \overline{J}_s | Alm$ Tangential components of H-fields are discontinued by an amount of surface current densities. (II) Using Crucis Law for H- bierd, Bni = Bnz. i-e. Normal component of magnetic blux ure continues across the interfuce. densities pasubolic enterna

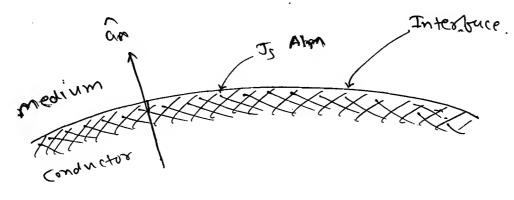
Field



PEC: Perfect electric Conductor

Js: (unrest per unit width (Alm)

Behaviour of Magnetic field Intensities cicross a conductor interfuce.



- E = NX NO
- -> Tangential Components of magnetic fields are earney to surface current density.
- @ Bn=0 (or) 4n=0.
 - -> Mosmal Components of magnetic brend intensities. are vanishes across the

conductor interface.

Js: Systyle Chosent density across the Conductor

I the plane y=0 Separates two mediums y < 0 is medium-1 and is characterised by y < 0 and y > 0 is medium-0 and is characterised by the characterised by y > 0 and y > 0 are interfered.

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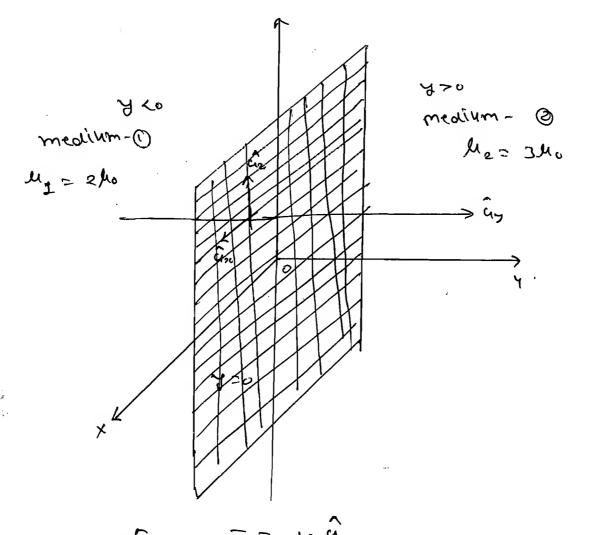
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<u>Α</u>~ι:



$$\begin{aligned}
\overline{H}_1 &= 10 \hat{\Omega}_2 & | \overline{H}_2 &= 10 \hat{\Omega}_{2L} \\
(\overline{H}_1 - \overline{H}_2) \times \hat{\Omega}_n &= \overline{J}_3 \\
\overline{J}_3 &= (10 \hat{\Omega}_2 - 10 \hat{\Omega}_{2L}) \hat{\Omega}_y \\
\overline{J}_3 &= -10 \hat{\Omega}_{2L} - 10 \hat{\Omega}_2 \cdot Alm.
\end{aligned}$$

```
Ex-2 Referring to the above figure
   Let, Fi = (3 ax + 4 ay + 5an) Alm
         Hz F
  assume cursent tree interface find B, Hz
        Bz
  and
       BI = MI [FI].
     : B1= 40[ cax + Bay + 1042).
   : H= 3 an + 4 ay + 5 az.
    : Fi = HEI QE + Hmi Qn.
   .. Ht = 30x + 502, Fm = 40y.
          HE, = HEZ ( ": 35=0)
 ~ NOW,
     (: turgentia components are esnal).
   H_{t_1} = 3\hat{q}_x + 5\hat{q}_z.
       Hz = HEZ QE + Hnz Qn.
                     (;; tszo).
         Bni = Bnz
      : 12 Hnz = H, Hn1.
      : Hnz = ly x hay.
        Hnz= 2 xhay
        :  fre = 8 ay
     H2 = 30, + $ Qy + 502.
```

$$B_2 = A_2 \overline{A_2}$$

$$B_2 = A_0 \left[g \hat{\alpha}_x + 8 \hat{\alpha}_y + 15 \hat{\alpha}_z^2 \right].$$

Ex-3 In the above Problem assume that the interface has non zero surface coment of $\overline{J}_{3} = (5\hat{q}_{x} + 10\hat{q}_{z}) Alm.$ Find

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Bil hz and

Hi= 30/2 + 40/2 + 50/2.

Bi= Mi Fi

Bi = 1 No [642 + 89y + 1042]

 μ_{0} ν_{0} ν_{0

KE, WE -[(Hti-Htz) gt + (Hni-Hnz) and x an = 5.

: (Her- Hez) (at xan) =].

 $\therefore \hat{q}_{t} = \frac{3}{\sqrt{2h}} \hat{q}_{x} + \frac{5}{\sqrt{2h}} \hat{q}_{z}.$

: an = 4 ay

 $\hat{\alpha}_{t} \times \hat{\alpha}_{n} = \frac{12}{\sqrt{3n}} \hat{\alpha}_{z} + \frac{20}{\sqrt{3n}} \hat{\alpha}_{x}.$

: $(H_{41}-H_{42})(\frac{12}{\sqrt{3}n}\hat{q}_2-\frac{20}{\sqrt{3}n}\hat{q}_x)=\frac{20}{\sqrt{3}n}\hat{q}_x$

1.12 (HE- HE2) = 10, -x6(ME7- HE2) = B.

 $\frac{1}{12} = \frac{8}{7} + \frac{9}{3} + \frac{9$

A Time Varying Fields:

The existing Amperers Law, when it is a provided to the time varying field in a non-conducting medium the Law is having Some inconsitency of unsatisfaction. This inconsitency is been eliminated by adding a new term Jo as follows:

TXH = Jc + Jo Modified Americs take D on both the side.

$$\nabla \cdot \nabla \times \vec{\mu} = \nabla \cdot \vec{J}_c + \nabla \cdot \vec{J}_o$$

.. Divergence of curr is zero.

C Dierectors)

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$$abla \cdot \overline{\mathcal{I}}_{\mathfrak{p}} = + \frac{35 v}{35 v}.$$

Jp is defined as time state of Change 151 or electric blux Density.

Je dominates en a conducting medium and is Zero in perfect Dielectric.

dominates in a diesectoic medium and is zero in perfect conductor.

The modified Ampere's Law is written Jc + Jo = PXH.

VXH = Jc + Jo.

 $\overline{J_C} = \overline{\sigma E} \quad Alm^2.$ $\overline{J_D} = \frac{\partial D}{\partial t} = \overline{E} \quad \overline{\partial E} \quad Alm^2.$

* Faouday's Law of Electromagnetic Conduction:

when a Steelin nary Conductor and by a moving magnetic trux therm on vice versue then emf will be induced. This induced emf will inturn produces a magnetic trux which opposes original trux [Lenz's Law). Mathametically we write

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$$\therefore \qquad \begin{cases} \vec{E} \cdot \vec{q} \cdot \vec{z} = -\frac{\delta F}{\delta \phi} \end{cases}.$$

W

$$: \oint \overline{E} \cdot d\overline{s} = -\frac{3}{24} \int \overline{B} \cdot d\overline{s}.$$

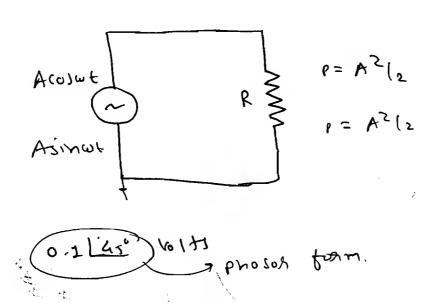
$$\int (\Delta \times \underline{E}) q_1 = -3 \text{Me} \int_{\overline{B}} \underline{B} \cdot q_2$$

$$\therefore \quad \sqrt{XE} = -\frac{M}{9B}$$

Deither Source is Acosat or Asimat

the average power deriver to 1 - resistor

is identically same which is equal to A2(2).



→ 0.1(0) (wt+ 45) (oh)

→ 0.1 sin (at+ 45).

-> or Im Core; (w++45)) (or)

7 Re[0.18

when the anantities are represented in

the phasor torm we suppresses the time

Variation tor the mathematical convinience

this time variations are approximated as

Cosine or sine or ejust.

 $\rightarrow E \rightarrow E(x, y_1 z_1^{x_1})$ (or) $E(y_1, x_1, z_1 t)$ of $E(y_1, y_1 t)$.

Light is a function of time and Space coordinates.

E= Re[Ex·ejut].

is called phasor token of E. $\overline{F}_{R} \rightarrow \overline{F}_{R} (\mathfrak{X}, \mathfrak{A}, \mathfrak{E}) (\mathfrak{g}_{R}) \overline{F}_{R} (\mathfrak{I}, \emptyset, \mathfrak{E}) (\mathfrak{g}_{R}) \overline{F}_{R} (\mathfrak{I}, \emptyset, \mathfrak{g}).$ spuce covodinates onit. tr. 06 Ly It is $\Delta \times \underline{e} =$ - 3B. $: \nabla \times \left[\operatorname{Re} \left\{ \overline{B}_{R} \cdot e^{j\omega t} \right\} \right] = - \frac{3}{4} \left[\operatorname{Re} \left\{ \overline{B}_{R} \cdot e^{j\omega t} \right\} \right].$: $\nabla \times \left[\text{Re} \left\{ \overline{E}_{R} \cdot e^{j\omega t} \right\} \right] = -j\omega \left[\text{Re} \left\{ \overline{E}_{R} \cdot e^{j\omega t} \right\} \right].$ bothe the side. Suppressing time Variation V x Fx = -jw Bx. 8/2 = jw = 5

Jak = 1/3.

_ <u>3</u> _	ī	, Gar	m &	<i>b</i> 7		155
Maxwell's Equation	7.5010	Gauss Lew box	Gramss Lucion but	Modified Amporis	Faraday's Law	Name of the
7 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2		Bidy 1	\$ 0. di = Oems = \	SHON = ((Tc+Tb) a)	103/22 = 1036 # W	re Integan form
X X V		女.百二0	V.01 5.6	25 + 35 = 1 25 + 25 = HX A	38- = 3×A	Point John
	十 ブル	V. B. 20.	V-05 - 55.	DXH, = JG + GZE.	DXEx= -jwax	Phasoz tom

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-> Maxwell had proved that any Electromagnetic baopiem con pe zoiner pa mind apare form cons. Ex-1 Lex D= (3x ax + ky ay + 72 az) nc/m² Assume Charge fore region. : V.o = Su But, Su=0. 3 +k + 7 = 0 : k=-11 wc/m3 \bigcirc Ex-2 Let, E= (kx-100+) Gy VIm, H= (x+20+) Go Alm. Assume M= 0.25 Hlm. $\nabla \times \vec{E} = -\lambda \frac{\partial \vec{h}}{\partial n}$. $= -20 \text{ M} \quad \text{a.} \quad \text{a.}$: K= -20x 1, : [k= -5 Ulm2]

* EM Waves:

=> Linear Medium:

A medium is Said to be linear in that medium DIE must have same discretion.

Aisortion (OR) BILL must have same discretion.

The does not mean that all are having same discretion.

Homogenius Medium:

→ Usually at high brequency medium is Characterised by M and E. It these are constant throughout the medium then the medium is said to be a homogening the medium.

=> Isotoopic Medium:

-> In this medium It wood & Scalar Constant.

In general, real part $\mathcal{L} = \begin{bmatrix} \mathcal{U}' - \mathcal{J} \mathcal{U}'' \\ \mathcal{E}'' - \mathcal{J} \mathcal{E}'' \end{bmatrix}$ $\mathcal{L} = \begin{bmatrix} \mathcal{U}' - \mathcal{J} \mathcal{L}'' \\ \mathcal{E}'' - \mathcal{J} \mathcal{E}'' \end{bmatrix}$ $\mathcal{L} = \begin{bmatrix} \mathcal{L} \mathcal{L} \mathcal{L} \\ \mathcal{L} \mathcal{L} \end{bmatrix}$ Thu. $\mathcal{L} = \begin{bmatrix} \mathcal{L} \mathcal{L} \mathcal{L} \\ \mathcal{L} \mathcal{L} \end{bmatrix}$ Part

- Real part of M&E indicate 1 storage Property of medium. -> Imaginary part 06 le & c indicate, disipiate Pooperty Ob medium. An Isotoopic medium is homogenius whereas homogening medium need not be 150 toopic. Charge free medium: Su=0
- Non- Conducting medium: == 0.
- * Unbounded Medium:
- These are no boundaries to meet in any disection.
- -> We assume that the wave is Propogating through a Lineur homogening isotropic Churge fore non- Conducting and unbounded medium.
 - >> Writing the maxwell's can fur the above assumed medium.
 - $\nabla x = \pi \frac{2}{3H}$
 - (1) $\nabla \times \overline{H} = E \frac{\partial \overline{E}}{\partial \overline{I}}$ (Non conducting meailum i) assumed 620).

 $(3) \quad \nabla \cdot \vec{0} = 0 \quad (-: \text{ Charge fore anedium i) eislamen}$ $\Rightarrow \quad \nabla \cdot \vec{E} = 0$

=> D. E=0 (: homogeneous medium is assumed).

 $\begin{array}{ll} (4) & \overline{V} \cdot \overline{\mu} = 0. \\ \overline{V} \cdot \overline{B} = 0. \end{array}$

-> Taking curs on 10 both the sides.

DX DX E = -MD X 3h.

· D(DE) - DSE = -M & (DXH).

=: $\nabla^2 \vec{E} = M \in \frac{82\vec{E}}{82^2}$, Vector wave en,

similiary tuking (not on @ both sides.

TH = UF 82H

-> For simplicity Let us solved the problem in

Carresian Coosainate.

> Expunding Gaveegn in Cartesian Constinents

These are $\frac{\partial^2 \vec{H}}{\partial x^2} + \frac{\partial^2 \vec{H}}{\partial x^2} + \frac{\partial^2 \vec{H}}{\partial x^2} = \frac{\partial^2 \vec{H}}{\partial x^2} = \frac{\partial^2 \vec{H}}{\partial x^2} + \frac{\partial^2 \vec{H}}{\partial x^2} + \frac{\partial^2 \vec{H}}{\partial x^2} = \frac{\partial^2 \vec{H}}{\partial x^2} + \frac{\partial^2 \vec{H}}{\partial x^2} + \frac{\partial^2 \vec{H}}{\partial x^2} = \frac{\partial^2 \vec{H}}{\partial x^2} + \frac{\partial^2 \vec{H}}{\partial x^2} + \frac{\partial^2 \vec{H}}{\partial x^2} + \frac{\partial^2 \vec{H}}{\partial x^2} = \frac{\partial^2 \vec{H}}{\partial x^2} + \frac{\partial^2 \vec{H}}{\partial x^2}$

→ E and H are Fr. of lime and Spure Coordinates. -> For simplicity Let in assumed that wave is propogeting along z-direction in unbounded medium. -> since there are no boundries to meet along X & Y disections. Then we Conclude the passical vasication of any bierd Component with respect to x and y i.e. spor ()=0, spox ()=0. -> the ear reduced to

 \bigcirc

(

0

 $\frac{\partial^2 E}{\partial z^2} = \frac{\lambda E}{\delta E}$ These and 2nd order $\frac{\partial^2 E}{\partial z^2} = \frac{\lambda E}{\delta E}$ $\frac{\partial^2 E}{\partial z^2} = \frac{\lambda E}{\delta E}$ $\frac{\partial^2 E}{\partial z^2} = \frac{\lambda E}{\delta E}$

-> We assumed Charge fee region:

V. E = O. $\frac{\partial x}{\partial (E^{2})} + \frac{\partial x}{\partial (E^{3})} + \frac{\partial z}{\partial (E^{5})} = 0.$

0 + 0 + dEz =0.

: Ez maj be Zeso (or) Constant.

-> Max. Vaine of D.D. = 1701.

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(OR)

Createst state of incoeuse.

* Angle bet The two sustaires:

> Let, Ø, (x,4,21= C, 8

Ø2 (x, 4, 21= C2

-: COSO = \[\forall \pa_1 \cdot \pa_2 \].

* For solenoides vector D.F=0.

* For Irrotational rector DXF=0.

* Crosen Theorem in a prame.

() \odot 9 **9** * Del operator (V).

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$$\rightarrow \nabla = \frac{\partial}{\partial x} \bar{\alpha}_{x} + \frac{\partial}{\partial y} \bar{\alpha}_{y} + \frac{\partial}{\partial z} \bar{\alpha}_{z}.$$

gradient 06 a sealar Fiela:

-> good V= TV = dv | max Gr.

: grud V= DV = dV Qx + dy Qy + de Qz.

* Divergence of a vector:

 $\nabla \cdot \overline{A} = \frac{\partial A_X}{\partial X} + \frac{\partial A_Y}{\partial Y} + \frac{\partial A_Z}{\partial Z}$

> VØ = 1 30 au + 1 30 au + 1 30 aw aw

To V. A = 1 [ou (h2h3Au) + ou (h3h1Ar) + ou (h1h2 Aw)]

TXA= hihzhz hina hzar hzar

(3)

$$\nabla^{2} \varphi = \frac{1}{h_{1}h_{2}h_{3}} \left[\frac{\partial}{\partial m} \left(\frac{h_{2}h_{3}}{h_{1}} \frac{\partial \varphi}{\partial m} \right) + \frac{\partial}{\partial v} \left(\frac{h_{1}h_{2}}{h_{2}} \frac{\partial \varphi}{\partial v} \right) \right]$$

$$+ \frac{\partial}{\partial m} \left(\frac{h_{1}h_{2}}{h_{3}} \frac{\partial \varphi}{\partial m} \right) \left[\frac{\partial}{\partial m} \left(\frac{h_{1}h_{2}}{h_{3}} \frac{\partial \varphi}{\partial m} \right) \right]$$

$$+ \frac{\partial}{\partial m} \left(\frac{h_{1}h_{2}}{h_{3}} \frac{\partial \varphi}{\partial m} \right) \left[\frac{\partial}{\partial m} \left(\frac{h_{1}h_{2}}{h_{2}} \frac{\partial \varphi}{\partial m} \right) \right]$$

$$+ \frac{\partial}{\partial m} \left(\frac{h_{1}h_{2}}{h_{3}} \frac{\partial \varphi}{\partial m} \right) \left[\frac{\partial}{\partial m} \left(\frac{h_{1}h_{2}}{h_{2}} \frac{\partial \varphi}{\partial m} \right) \right]$$

$$+ \frac{\partial}{\partial m} \left(\frac{h_{1}h_{2}}{h_{3}} \frac{\partial \varphi}{\partial m} \right) \left[\frac{\partial}{\partial m} \left(\frac{h_{1}h_{2}}{h_{2}} \frac{\partial \varphi}{\partial m} \right) \right]$$

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$$+ \frac{\partial}{\partial m} \left(\frac{h_{1}h_{2}}{h_{3}} \frac{\partial \varphi}{\partial m} \right) \left[\frac{h_{1}h_{2}}{h_{3}} \frac{\partial \varphi}{\partial m} \right]$$

$$+ \frac{\partial}{\partial m} \left(\frac{h_{1}h_{2}}{h_{3}} \frac{\partial \varphi}{\partial m} \right) \left[\frac{h_{1}h_{2}}{h_{3}} \frac{\partial \varphi}{\partial m} \right]$$

$$+ \frac{\partial}{\partial m} \left(\frac{h_{1}h_{2}}{h_{3}} \frac{\partial \varphi}{\partial m} \right) \left[\frac{h_{1}h_{2}}{h_{3}} \frac{\partial \varphi}{\partial m} \right]$$

$$+ \frac{\partial}{\partial m} \left(\frac{h_{1}h_{2}}{h_{3}} \frac{\partial \varphi}{\partial m} \right) \left[\frac{h_{1}h_{2}}{h_{3}} \frac{\partial \varphi}{\partial m} \right]$$

$$+ \frac{\partial}{\partial m} \left(\frac{h_{1}h_{2}}{h_{3}} \frac{\partial \varphi}{\partial m} \right) \left[\frac{h_{1}h_{2}}{h_{3}} \frac{\partial \varphi}{\partial m} \right]$$

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$$+ \frac{\partial}{\partial m} \left(\frac{h_{1}h_{2}}{h_{3}} \frac{\partial \varphi}{\partial m} \right) \left[\frac{h_{1}h_{2}}{h_{3}} \frac{\partial \varphi}{\partial m} \right]$$

$$+ \frac{\partial}{\partial m} \left(\frac{h_{1}h_{2}}{h_{3}} \frac{\partial \varphi}{\partial m} \right) \left[\frac{h_{1}h_{2}}{h_{3}} \frac{\partial \varphi}{\partial m} \right]$$

$$+ \frac{\partial}{\partial m} \left(\frac{h_{1}h_{2}}{h_{3}} \frac{\partial \varphi}{\partial m} \right) \left[\frac{h_{2}h_{3}}{h_{3}} \frac{\partial \varphi}{\partial m} \right]$$

$$+ \frac{\partial}{\partial m} \left(\frac{h_{1}h_{2}}{h_{3}} \frac{\partial \varphi}{\partial m} \right) \left[\frac{h_{1}h_{2}}{h_{3}} \frac{\partial \varphi}{\partial m} \right]$$

its magnitude, 165 * Unit Vector, Vector und → CAB = $\overline{AB} = (x_2 - x_1) \hat{a}_{31} + (y_2 - y_1) \hat{a}_{31} + (y_2 - y_1) \hat{a}_{21}$ -> |AB| or AB= N(x2-x1)2+ (72-71)2+ (22-71)2 * Scarar or Dot Product: ABCOSO. where 0 = angre bet A &B of Povjection: Length PE Length of projection rength of projection = Q. ap projection = (cr. ap) ap Vector $= \frac{\widehat{G} \cdot \widehat{F}}{\mathbb{F}^2} \times \widehat{F}.$ Cooss Producti

 \mathcal{O}

AXB = -BXA AXB = ABSIND Qn Application of (805) product: of parallelogoum = | AB x Ac |. Area of the toiunge ABC = 1 | AB X AC | * Scular Toiple Product: $\bar{A} \times (\bar{B} \times \bar{c}) = \bar{A} \cdot \bar{c} (\bar{g}) - \bar{A} \cdot \bar{g} (\bar{c}).$ $\Rightarrow \overline{A \cdot B} \times \overline{C} = \begin{cases} A_{x} & A_{y} & A_{z} \\ B_{x} & B_{y} & B_{z} \end{cases}$ $C_{x} \quad C_{y} \quad C_{z}$

Coordinates Systems:

2.

Carterian (or) rectangular (overlinete System coordinate Chindrical

Spherical Coordinate System. 3(Cartesium (09) Rectungular Coordinate System. 167 -> Any point in cartesium system is the intersection of x= constant, y= constand und the z = constant planes. point in Curtesian Statem = P(x11/2) Unit rectors are ax, ax, az. q= qxq2,qs ('5 - dī = dx qx + dy qy + dz cīz. (") -> ds= dydz qn (x= constant) ()(=) ds= dzdx ay (y= constant). ds= dx ay az (z= construt). -> dv= dxdyds . 100 2 Cylinarical System: ()Point is (\$, \$, \$). ()Unit rectus ag, an, az. -> Dibberential lengths are de, gode, ar. () () di= dy ug + yodø ug + jedzûz. --> ds= 8 død2 q. (8= constant). ds = dsdr qo (Ø = Constant).

ds = sdødø å, (22 constant).

Spresical coordinate system: b (21.6.18). a, a, a, de, ado, ssino 82 sin 0 do do Gr. (n= (onstant) Ssind drd & Go = (0 = Constart). = 2b δ do do \hat{a}_{g} (g = constant). drag + Rdoqo + Rsino do Go. Tours for mation form curtesium to mindrica and vice vessa: ve ctoh X = 3 COSX Cosa -sing 1 = 3 sino ay. |sing (05% 0 8= 1×5+45 [B], = [AT][B]x Ø = tan' (81x) Towns tomaction of vector town to spherica or vice verga: x= 2 sino. cos & y= 8 sino. sino - sim & \bigcirc CO19 COZ& ax: Sinocosa ay. SINO SINO COSO SIN 8= 1×2+y2+22 0 = (os' (=12) 0 Mil _ .0010 Ø= fun' (dlx).